

# SOI and symmetry: Lifting the Kramers' degeneracy

1.  $E(\mathbf{k}, \uparrow) = E(-\mathbf{k}, \downarrow)$  **time-reversal symmetry**

2.  $E(\mathbf{k}, \uparrow) = E(-\mathbf{k}, \uparrow)$  **inversion symmetry**

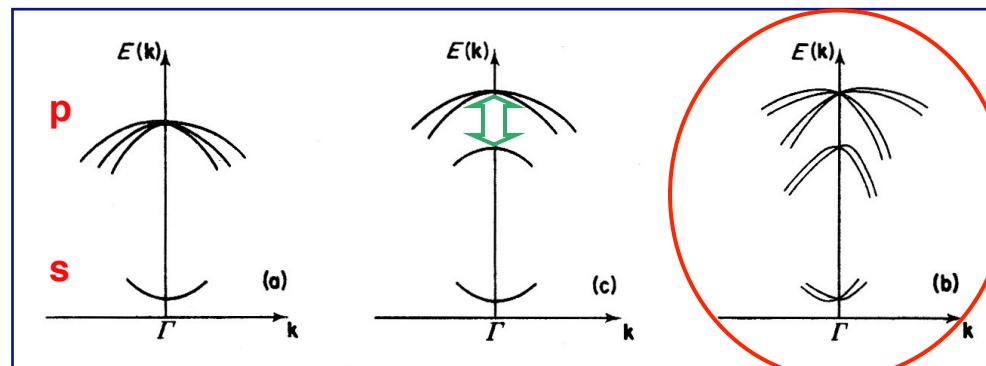
1+2.  $E(\mathbf{k}, \uparrow) = E(\mathbf{k}, \downarrow)$  **Kramers' degeneracy**

In the bulk of a non-CS solid or at the surface, inversion symmetry is broken

With SO interaction:  $E(\mathbf{k}, \uparrow) \neq E(\mathbf{k}, \downarrow)$

without external magnetic field

Except at  $\Gamma$  and at a few other “special” (TRI) points



no SO

with SO

SO - no inversion

Rashba and Dresselhaus effects

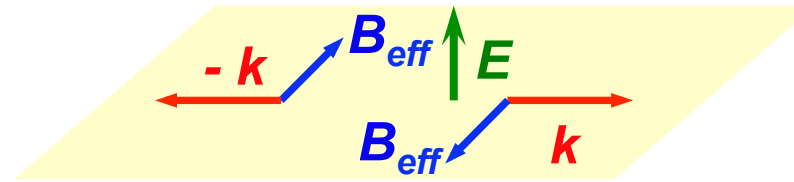
# The Rashba effect in a 2DEG

Free electrons at the surface  
“see” an electric field

$$\vec{E} = -\nabla V = -\frac{dV}{dz}\vec{e}_z$$

and a magnetic field

$$\vec{B}_{eff} = \frac{1}{c^2}\vec{v} \times \vec{E} = \frac{\hbar}{m^*c^2}\vec{k} \times \vec{E}$$



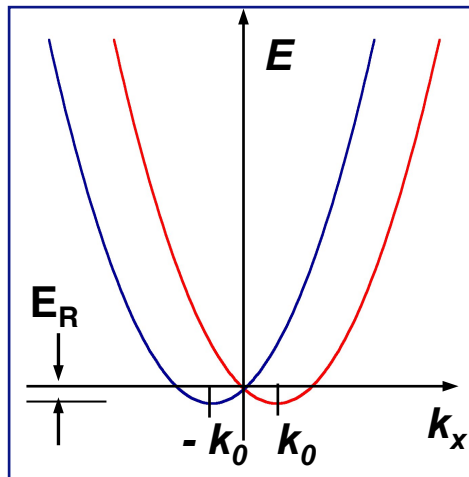
**Zeeman coupling**

$$H_{SOC} \approx -\vec{\mu}_S \cdot \vec{B} = \alpha_R (\vec{e}_z \times \vec{p}) \cdot \sigma$$

**The quantization axis is linked to k**



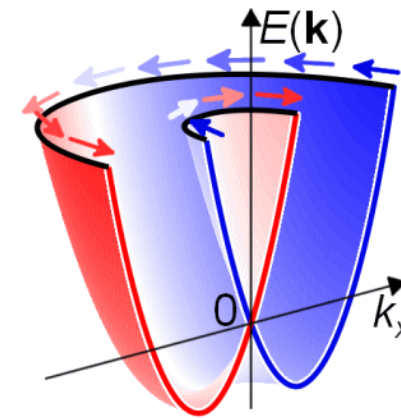
E. Rashba



$$E = \frac{\hbar^2 k^2}{2m^*} \pm \alpha_R k$$

$$E_R = |E(\pm k_0)|$$

$$\alpha_R \approx E \quad k_0 = \frac{m^* \alpha_R}{\hbar^2}$$



**Spin polarization**

**The expected Rashba energy  $E_R$  is very small:  $E_R \sim 10^{-6}$  eV!**

# Rashba vs. Zeeman

External in-plane **B**

$$\begin{pmatrix} \frac{\hbar^2(k_x+k_y)^2}{2m^*} & -iE_P \\ iE_P & \frac{\hbar^2(k_x+k_y)^2}{2m^*} \end{pmatrix}$$

$$E_P = -\mathbf{M} \cdot \mathbf{B}$$

“Effective” in-plane **B**

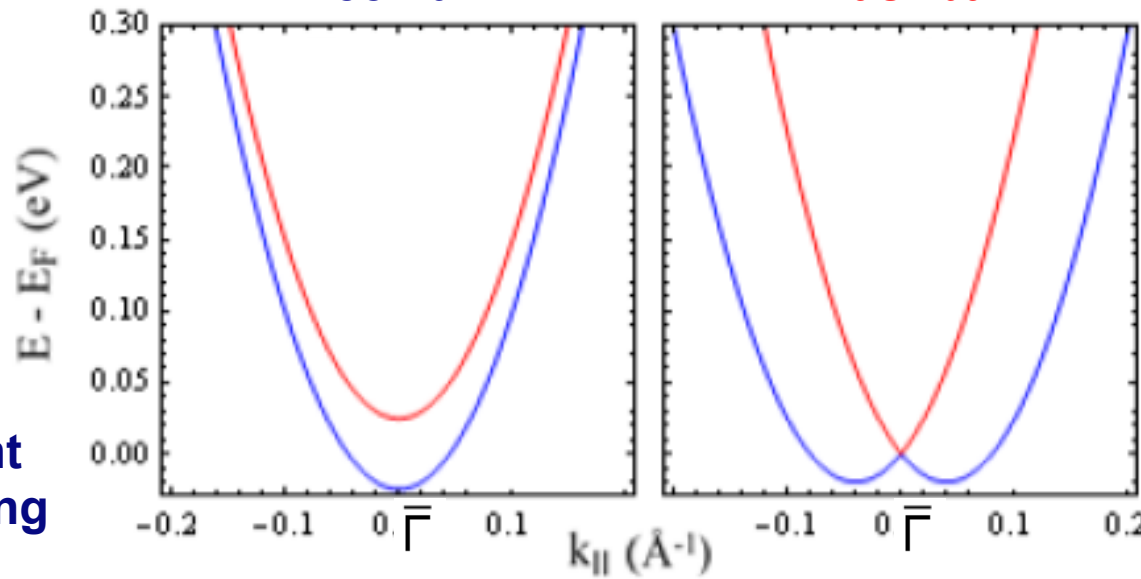
$$\begin{pmatrix} \frac{\hbar^2(k_x+k_y)^2}{2m^*} & \alpha_R(-ik_x - k_y) \\ \alpha_R(ik_x - k_y) & \frac{\hbar^2(k_x+k_y)^2}{2m^*} \end{pmatrix}$$



**Zeeman**



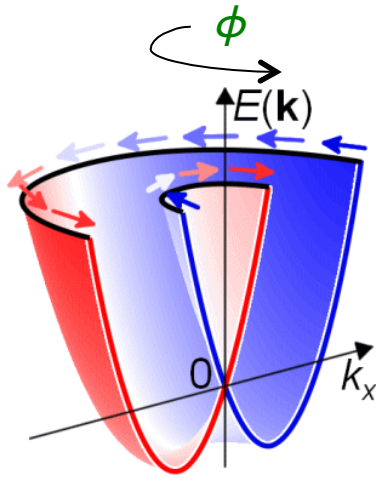
**Rashba**



**Constant  
E-splitting**

**k-linear  
E-splitting**

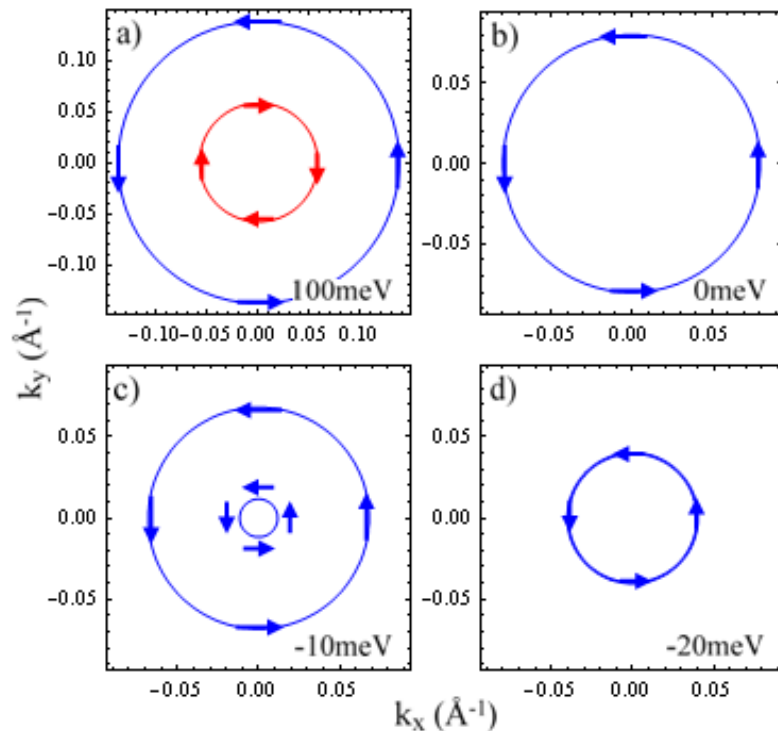
# The spin polarization



**SO mixes UP and DOWN spins**

$$|\psi_+(\vec{k})\rangle = \frac{e^{i(k_x x + k_y y)}}{2^{1/2}} (|\uparrow\rangle + e^{i\phi(k)} |\downarrow\rangle) \quad \text{Upper branch}$$

$$|\psi_-(\vec{k})\rangle = \frac{e^{i(k_x x + k_y y)}}{2^{1/2}} (|\uparrow\rangle - e^{i\phi(k)} |\downarrow\rangle) \quad \text{Lower branch}$$



$$\langle \sigma_x \rangle_{\pm} = \pm \cos \phi(k) ;$$

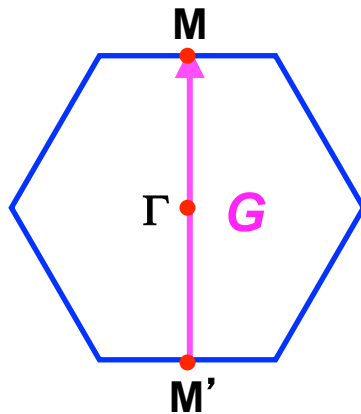
$$\langle \sigma_y \rangle_{\pm} = \pm \sin \phi(k) ;$$

$$\langle \sigma_z \rangle_{\pm} = 0$$

**Spin polarization**

# Time Reversal Invariant points

## Hexagonal symmetry



$$E(\vec{k}, \uparrow) = E(-\vec{k}, \downarrow) \quad \text{TR symmetry}$$

$$k = 0 \rightarrow E(\Gamma, \uparrow) = E(\Gamma, \downarrow)$$

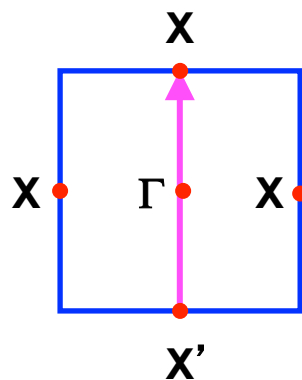
$$E(M, \uparrow) = E(M', \downarrow) \quad \text{TR symmetry}$$

$$E(M', \downarrow) = E(M' + \vec{G}, \downarrow) = E(M, \downarrow)$$

$$E(M, \uparrow) = E(M, \downarrow)$$

Translational  
symmetry

## Square symmetry



$$E(X, \uparrow) = E(X', \downarrow) \quad \text{TR symmetry}$$

$$E(X', \downarrow) = E(X' + \vec{G}, \downarrow) = E(X, \downarrow)$$

$$E(X, \uparrow) = E(X, \downarrow)$$

Translational  
symmetry

# Spin manipulation without magnetic fields

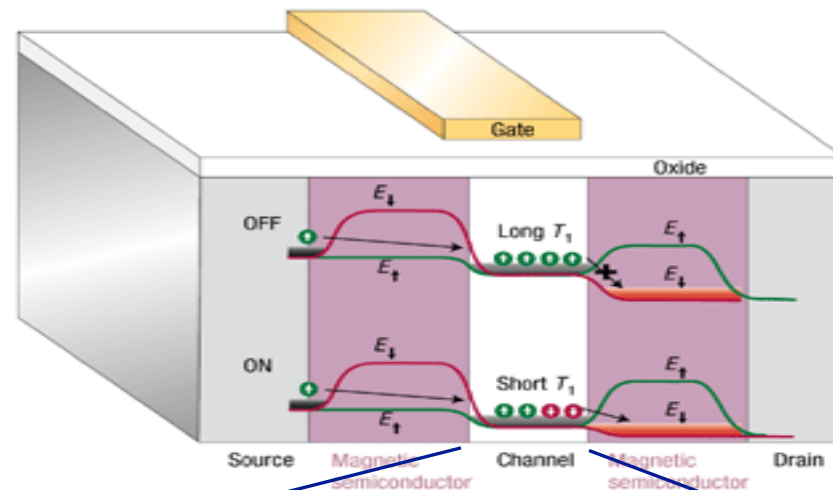
Polarized electrons are injected in a mixed  $|up\rangle + |down\rangle$  spin state.

The spin precesses along the channel:  $\Delta\theta \approx L\alpha_R$

It can be modulated by  $V_G$

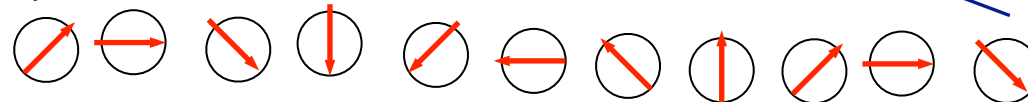
## The “spin transistor”

S. Datta and B. Das,  
APL 56, 665 (1990).



Awschalom and Flatté,  
Nature Phys. 3, 153 (2007).

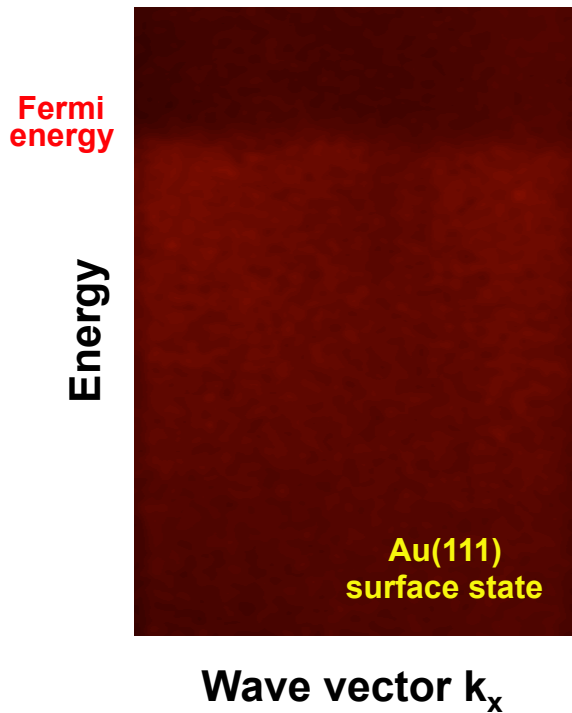
$E_{\uparrow}$  ———  
Rabi  
oscillations  
 $E_{\downarrow}$  ———



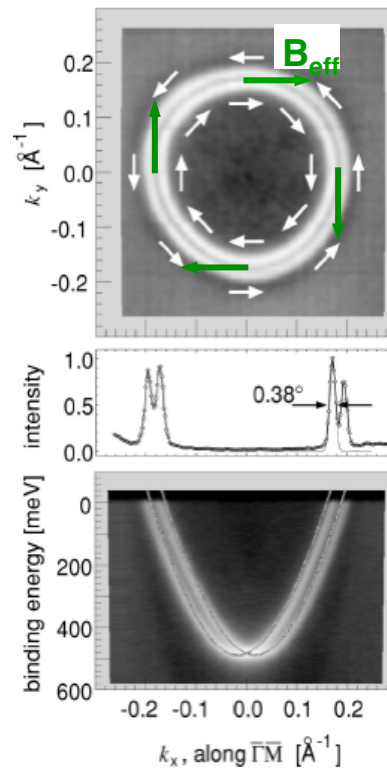
For InGaAs/InAlAs heterojunctions:  $L(\Delta\theta = \pi) \approx 0.5 \mu\text{m}$

# Shockley state at the Au(111) surface : ARPES

The circular Fermi surface is split into two spin-polarized branches



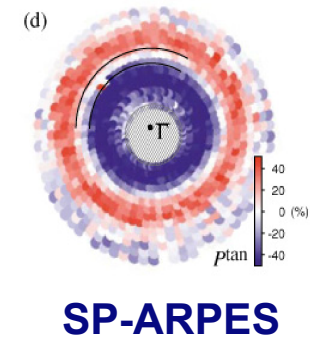
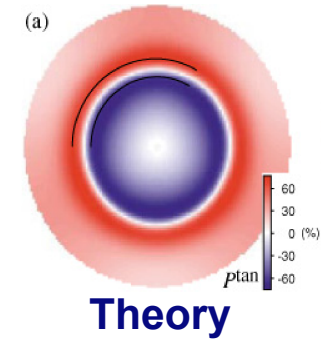
LaShell et al., PRL (1997).  
Reinert et al., PRB (2001).



$k_0 = 0.012 \text{ \AA}^{-1}$   $E_R \sim 2 \text{ meV}$

**LARGE !**

## Spin polarization

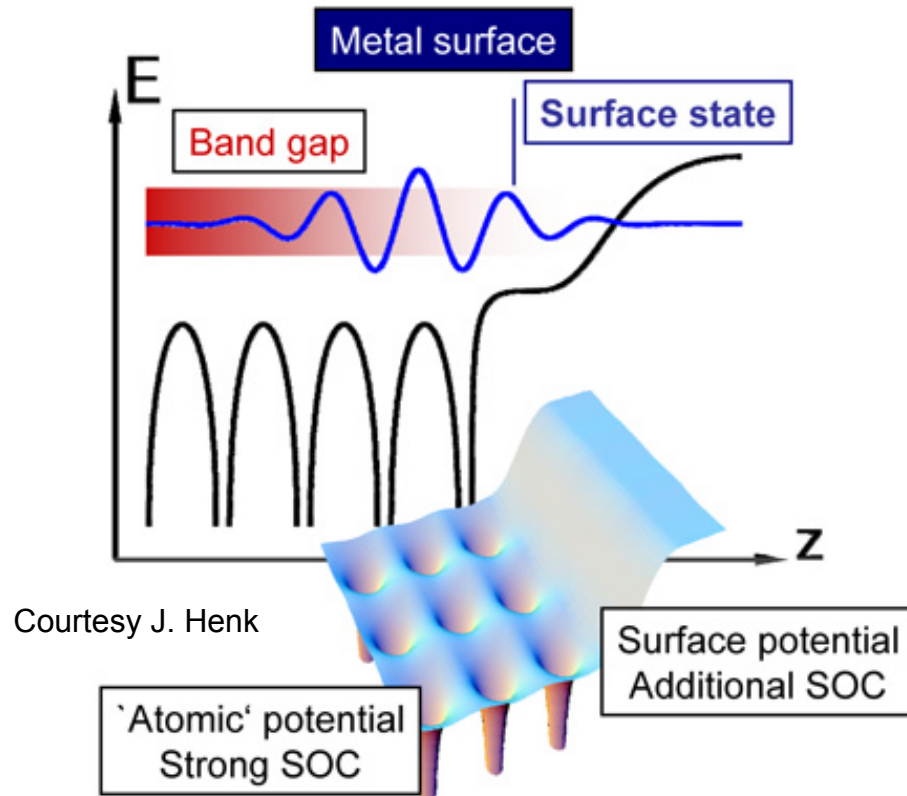


M. Hoesch et al., (2004)

# Much stronger fields near the nuclei !

The E field is largest near the nuclei

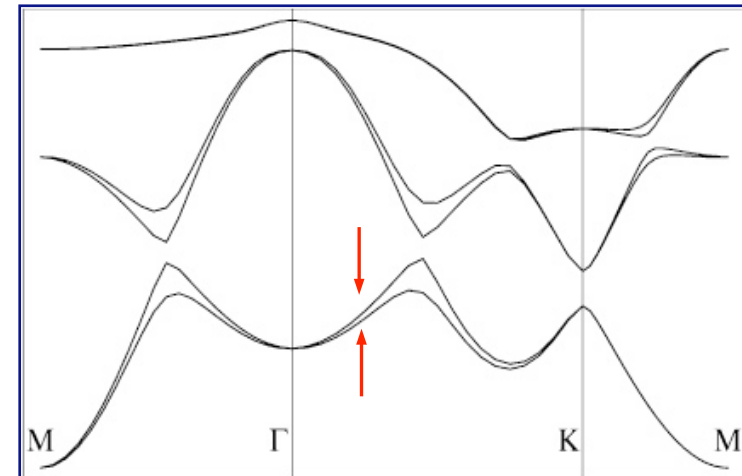
The intra-atomic SO interaction  
MUST be important



atomic SO parameter

surface term

$$\alpha_R \approx \alpha_{AT} \cdot \left( \frac{dV}{dz} \right)$$

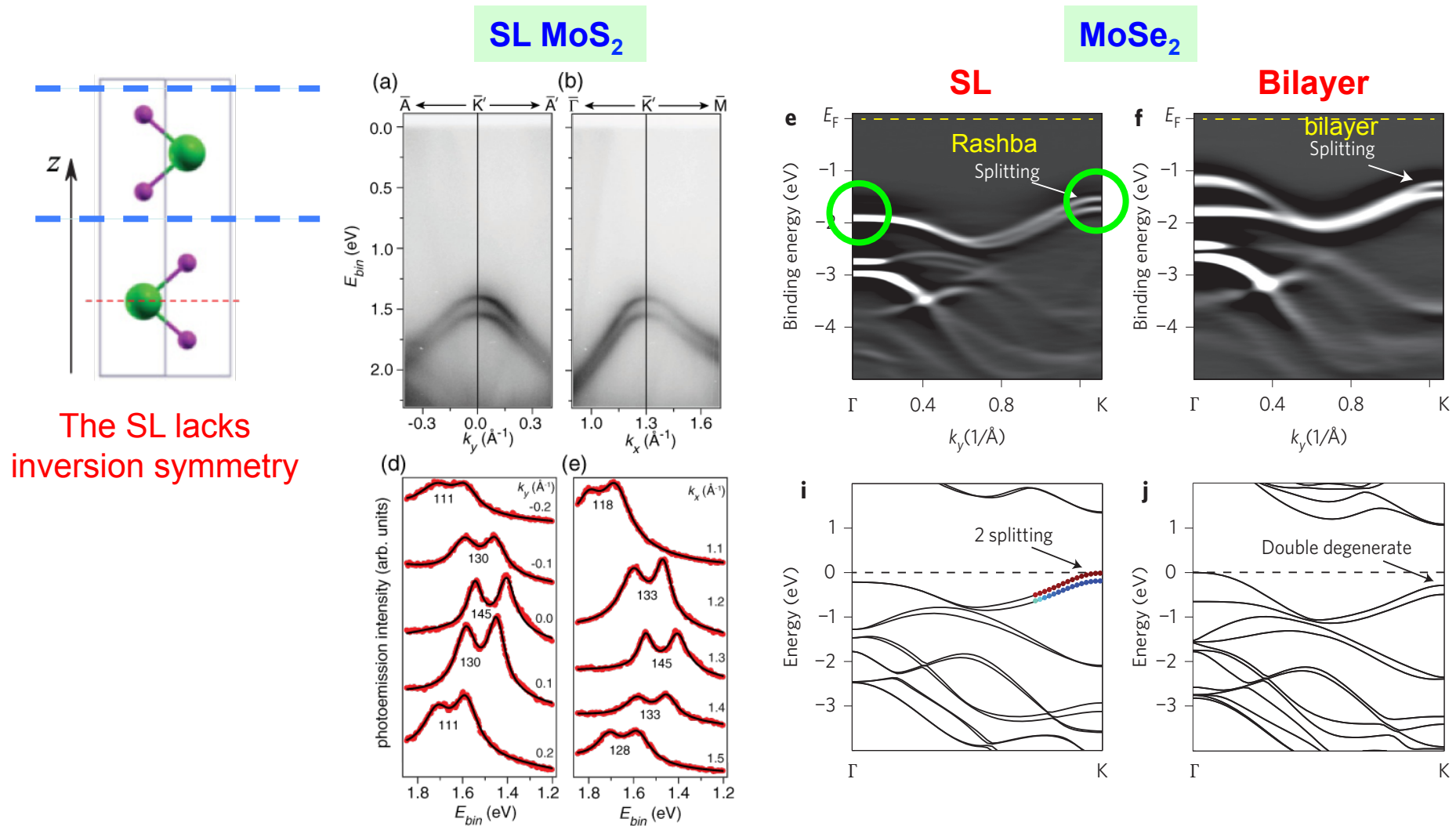


L. Petersen and P. Hedegård,  
Surf. Sci. **459**, 49 (2000)

Much larger splittings are possible



# Single-layer solids - ARPES

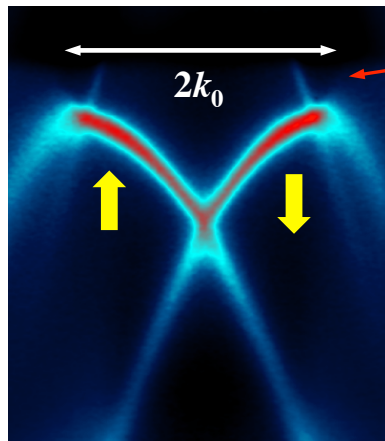
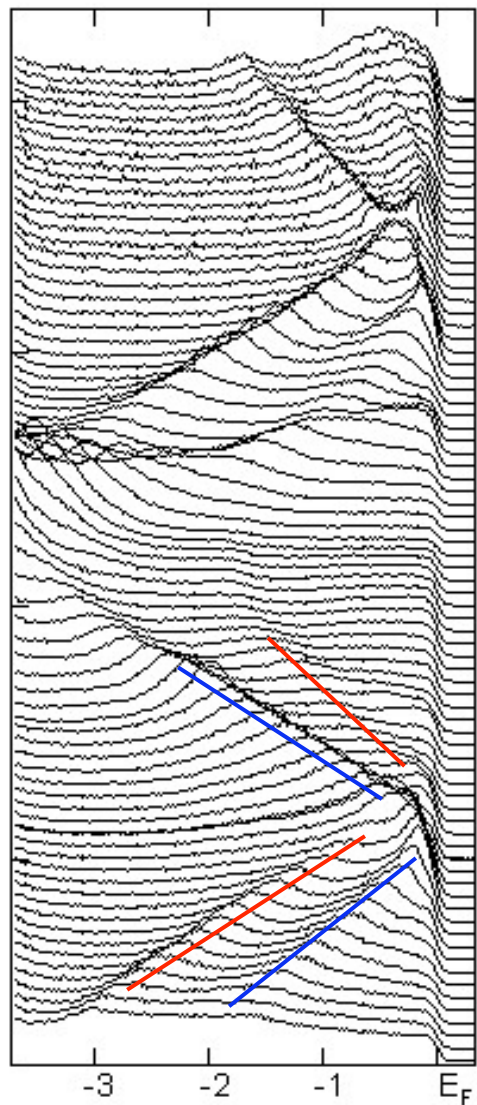


J.A. Miwa et al., PRL **114**, 046802 (2015)

Y. Zhang et al., Nat. Nanotech. **9**, 111 (2014)

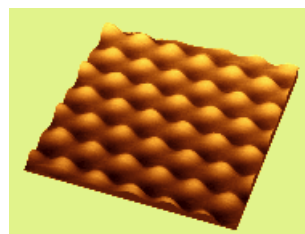
# Surface alloys with high-Z elements: Bi/Ag(111)

Ast et al., Phys. Rev. Lett. **98**, 186807 (2007)

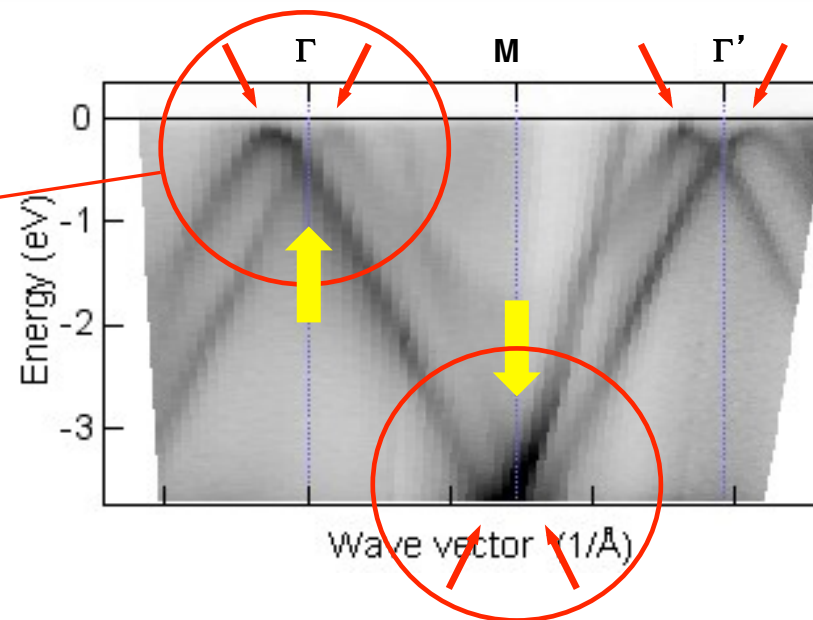
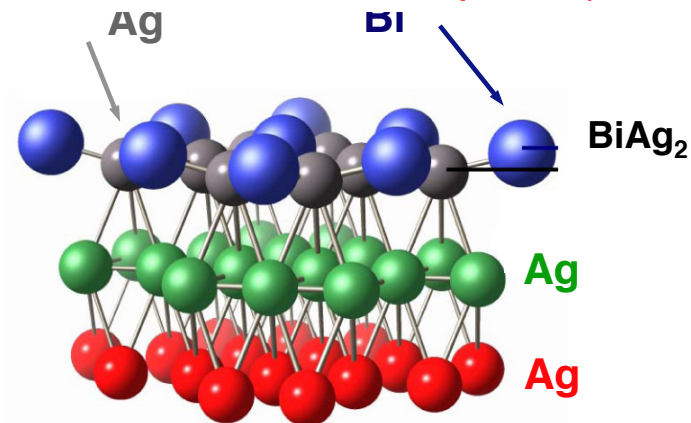
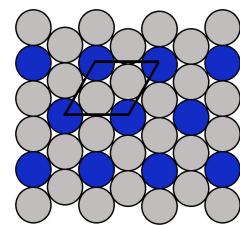


$E_R = 200 \text{ meV}$

**GIANT !**



STM

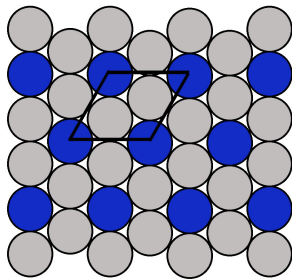
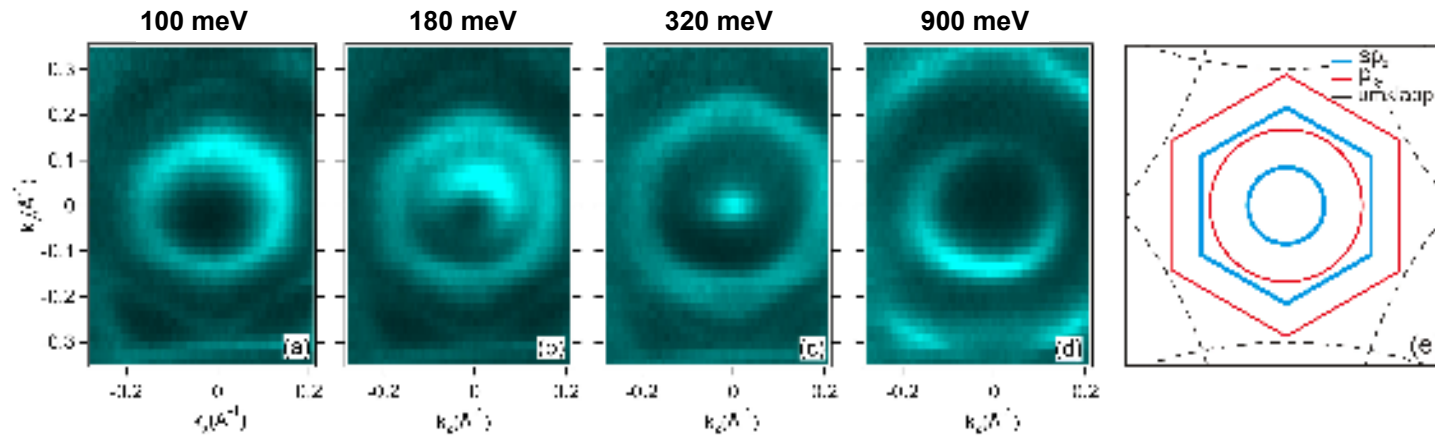


Surface bands degenerate at  $\Gamma$  and M (time-reversal invariant points)

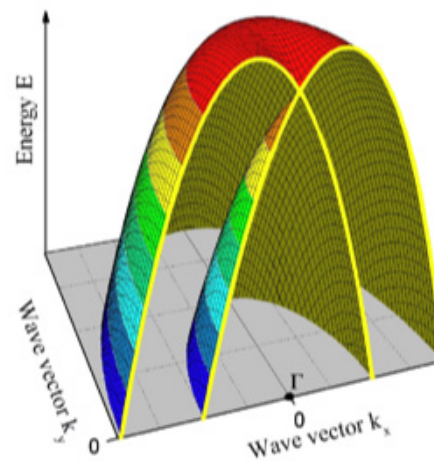
C.R. Ast et al., PRL **98**, 186807 (2007)

# In-plane symmetry breaking and anisotropy

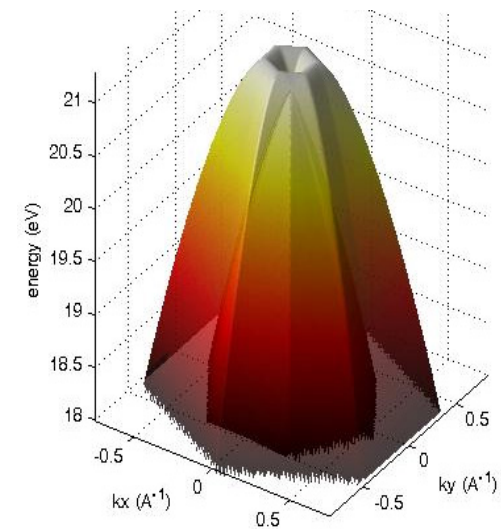
## ARPES constant energy cuts in k-space



Unlike the case of Au(111) the spin-split FS is clearly influenced by the crystal potential in-plane gradient

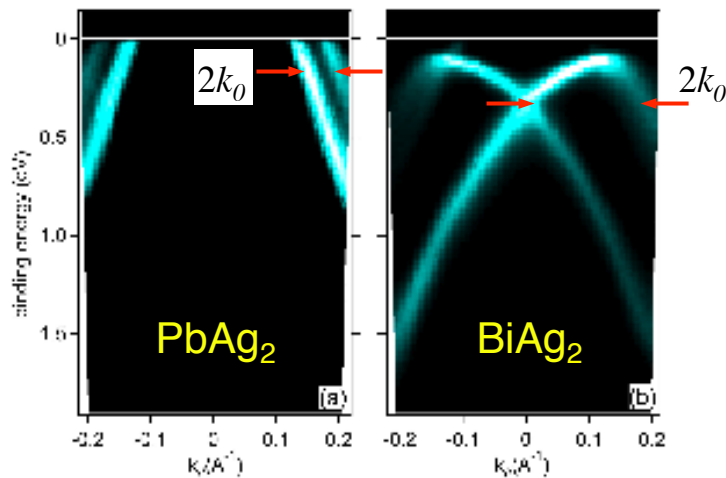
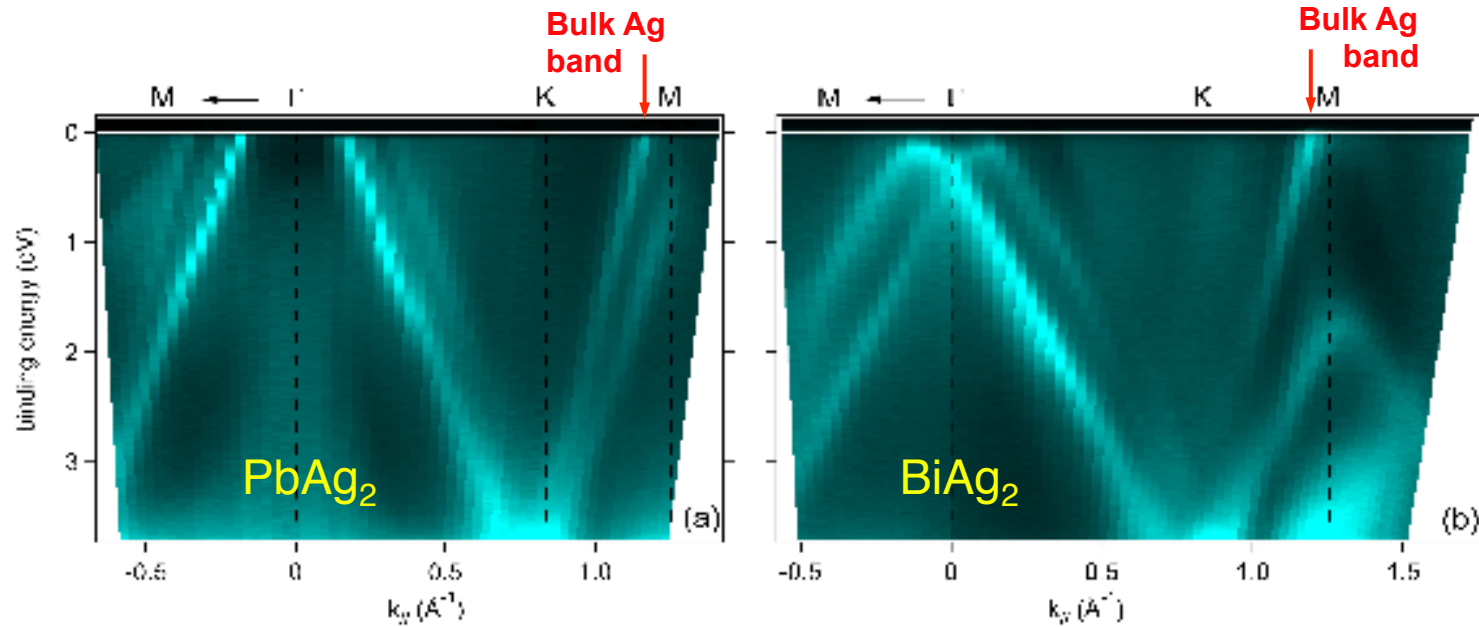


Simple ( Au(111) )



More realistic

# Turning the band-filling knob: Pb-Ag(111)



**Same structure: BiAg<sub>2</sub> surface alloy**

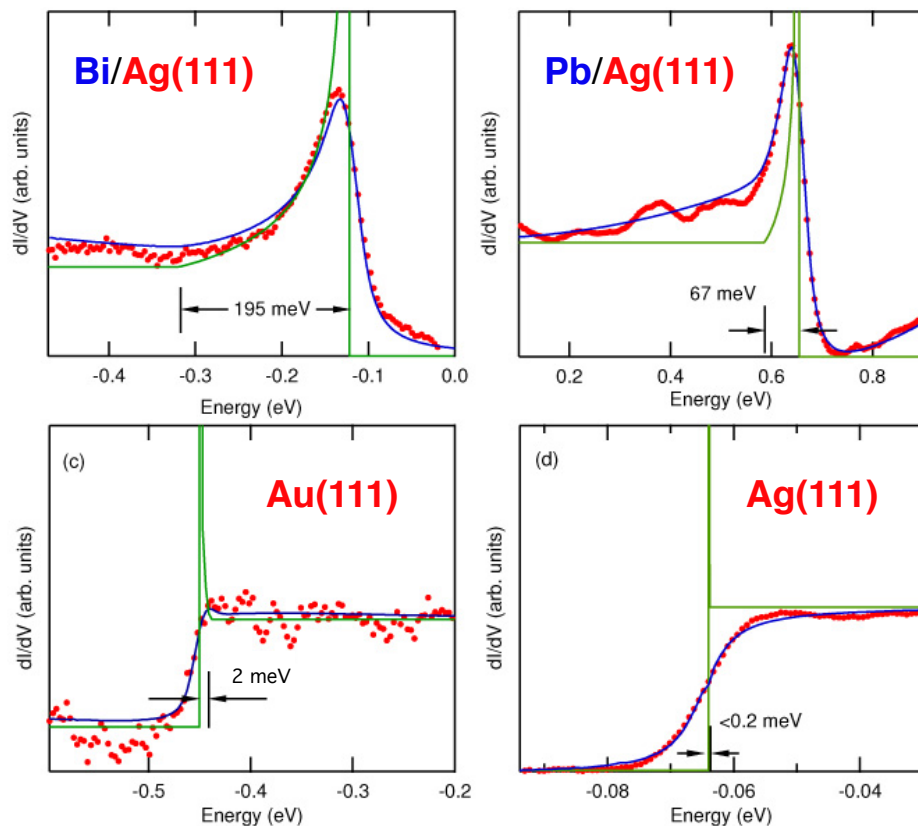
**Rigid band shift** to accommodate the extra electron

The **splitting** of the bands increases by a **factor 4** between PbAg<sub>2</sub> and BiAg<sub>2</sub> (the atomic SO parameter is 40% larger)

# Spin splitting and the density of states

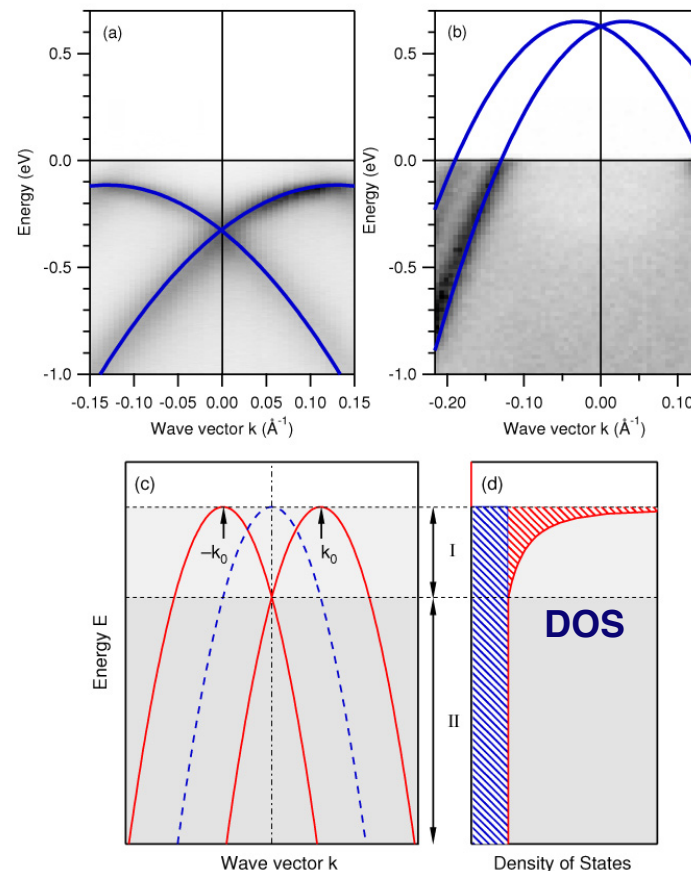
## Signatures of spin-split states in tunneling spectra

STS: MPI Stuttgart



**Bi/Ag(111)**

**Pb/Ag(111)**

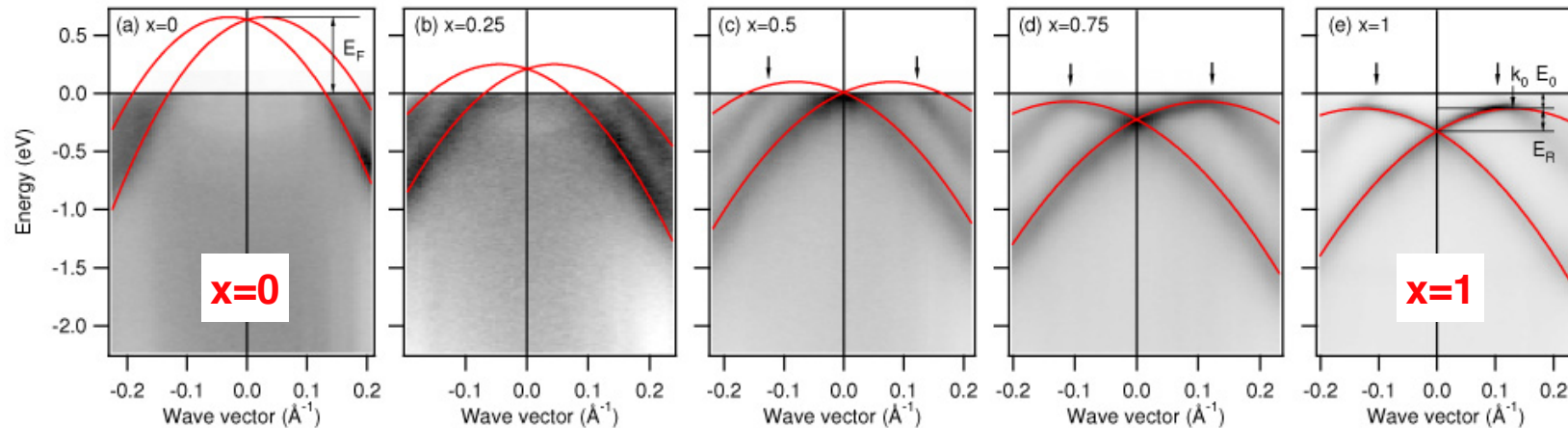


Ast et al., Phys. Rev. B. **75**, 201401(R) (2007)

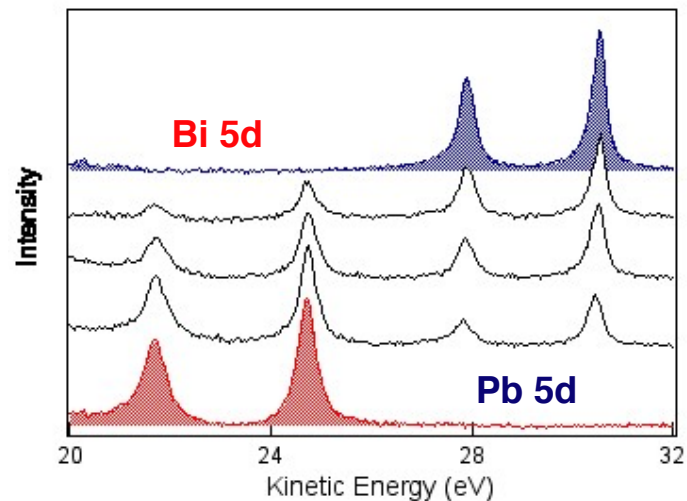
**"1D-like divergence"**

# Chemical tuning of $E_F$ and of the SO splitting

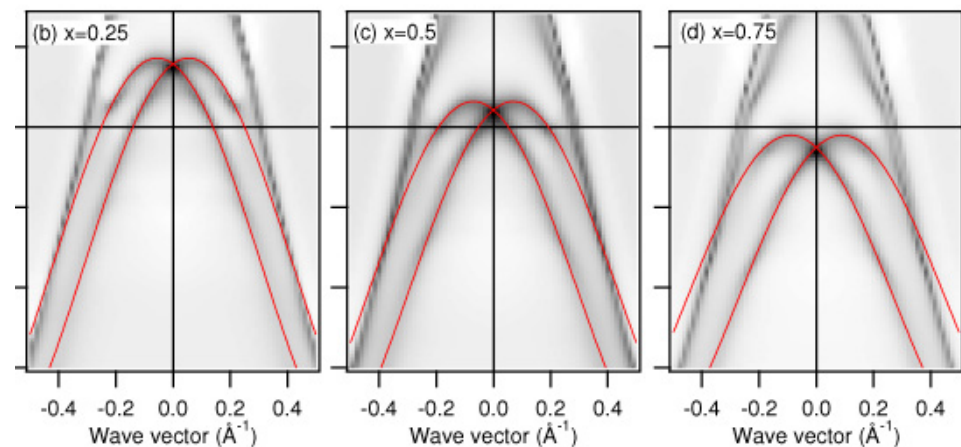
## $(\text{Bi}_x\text{Pb}_{1-x})\text{Ag}_2$ ordered alloys



### Internal calibration from core levels



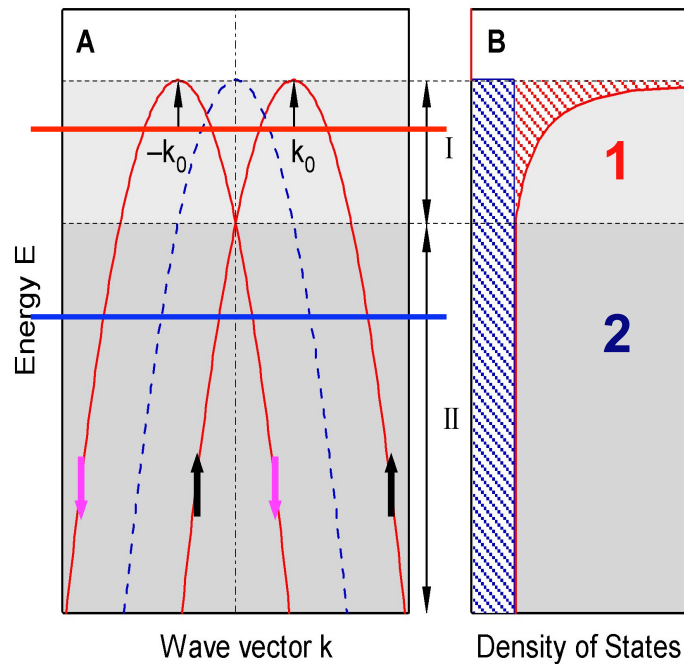
### THEORY (J. Henk)



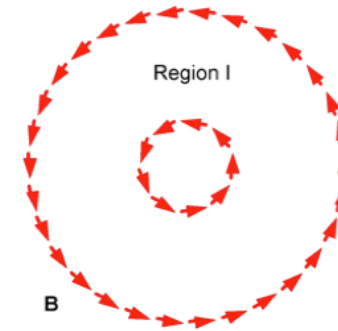
# Adjusting the spin pattern by interface engineering

## The spin pattern varies along the split band

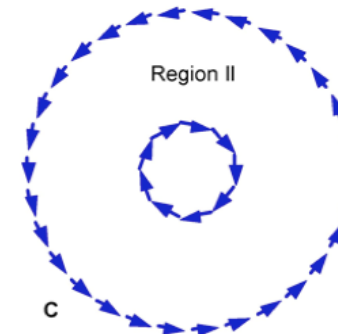
Two different situations are realized by tuning  $E_F$  through the band as a function of stoichiometry



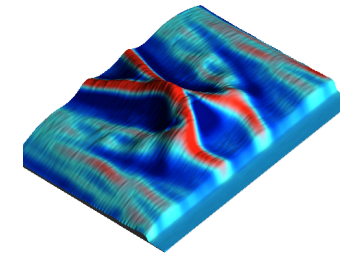
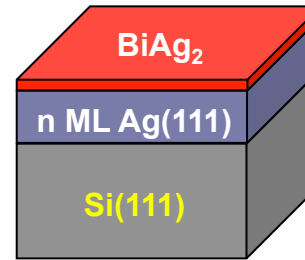
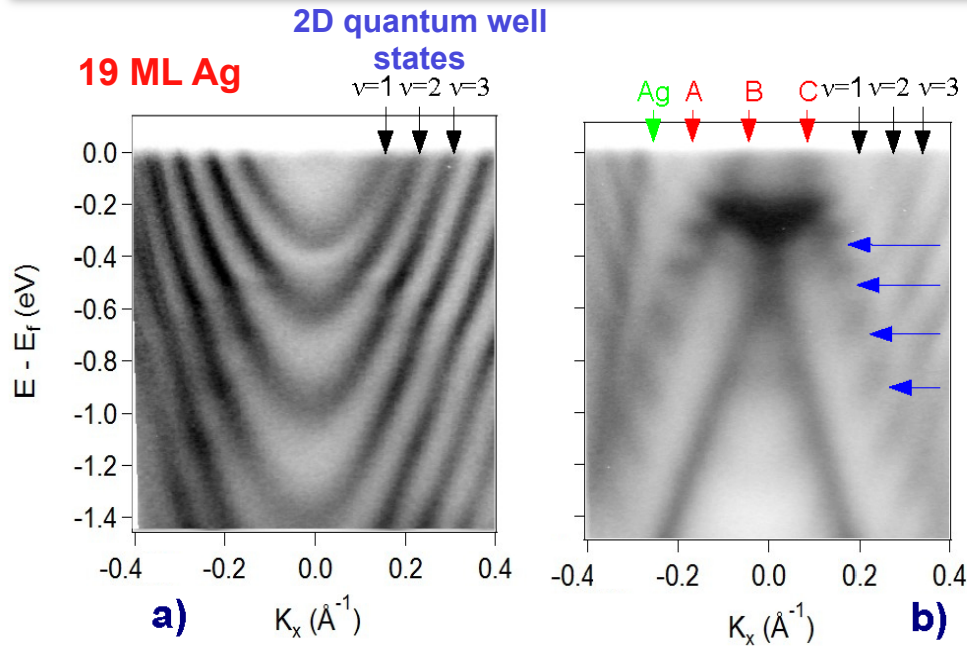
(1) chiral



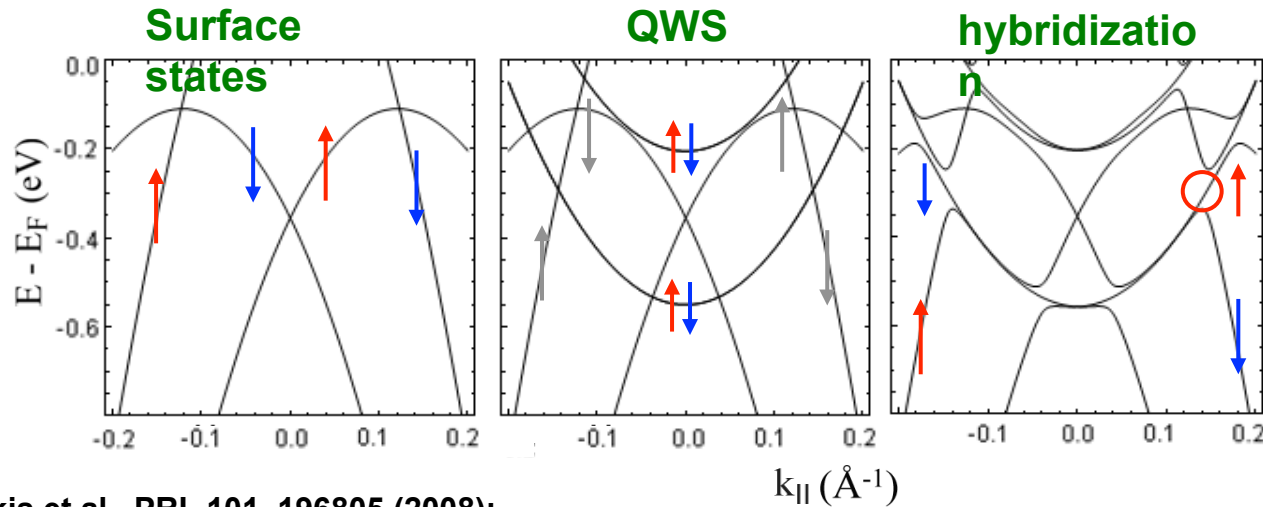
(2) non-chiral



# Thin Ag layer : quantum well states



- The QWS are also spin-polarized (negligible splitting)
- Only states of same spin can hybridize
- Fully polarized states in hybridization gaps

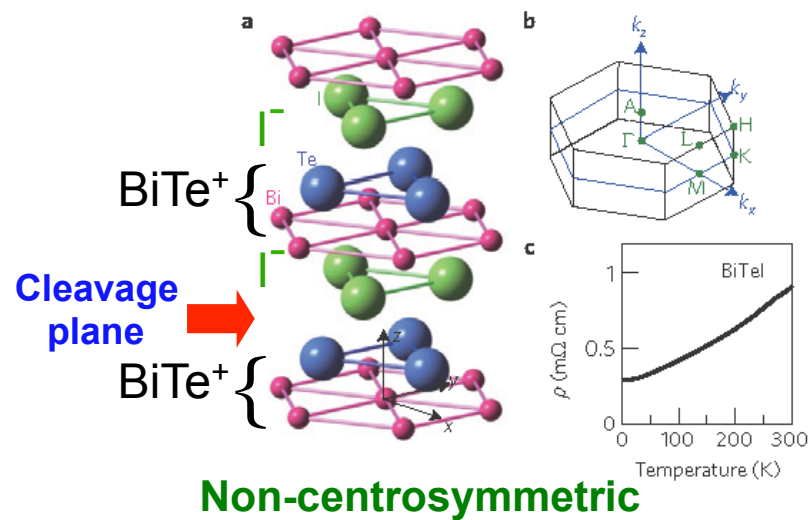


E. Frantzeskakis et al., PRL 101, 196805 (2008);

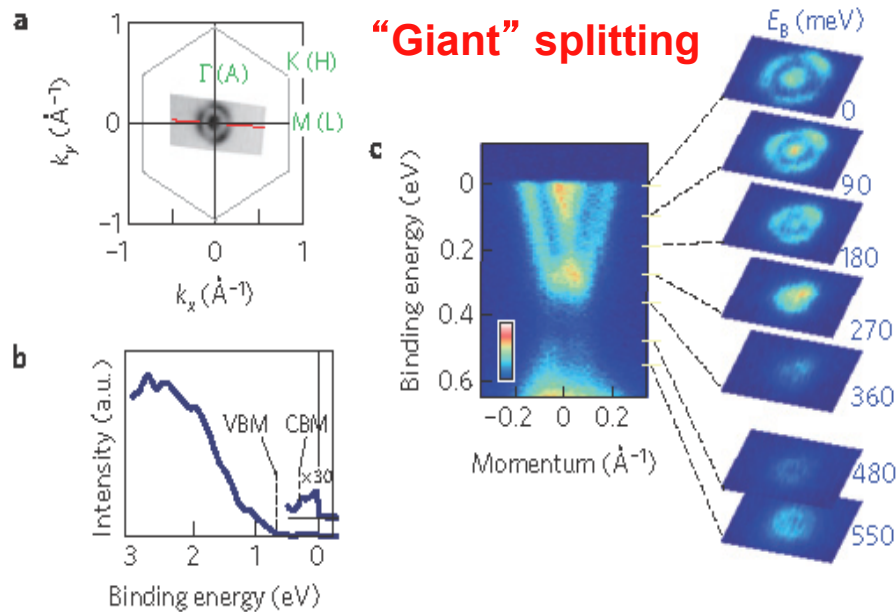
K. He et al., PRL 101, 107604 (2008).



# BiTeI: Rashba *and* Dresselhaus

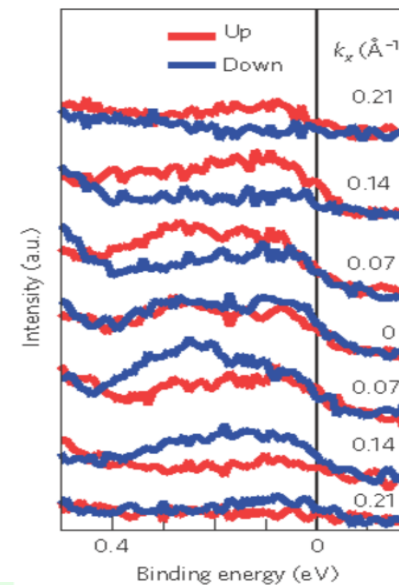
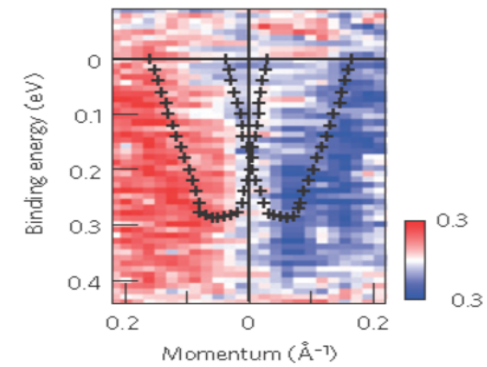


**Non-centrosymmetric**



**"Giant" splitting**

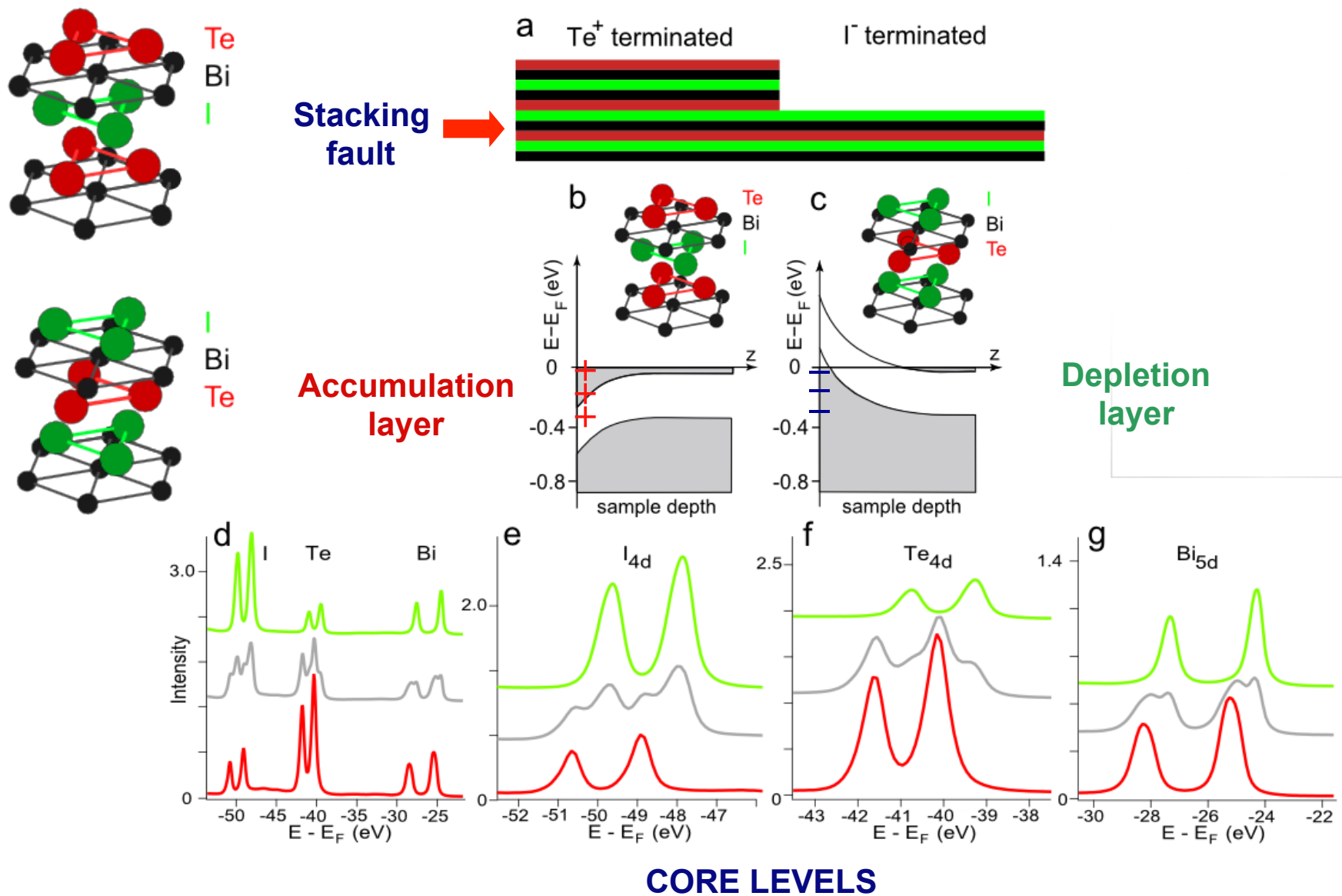
**SP-ARPES**



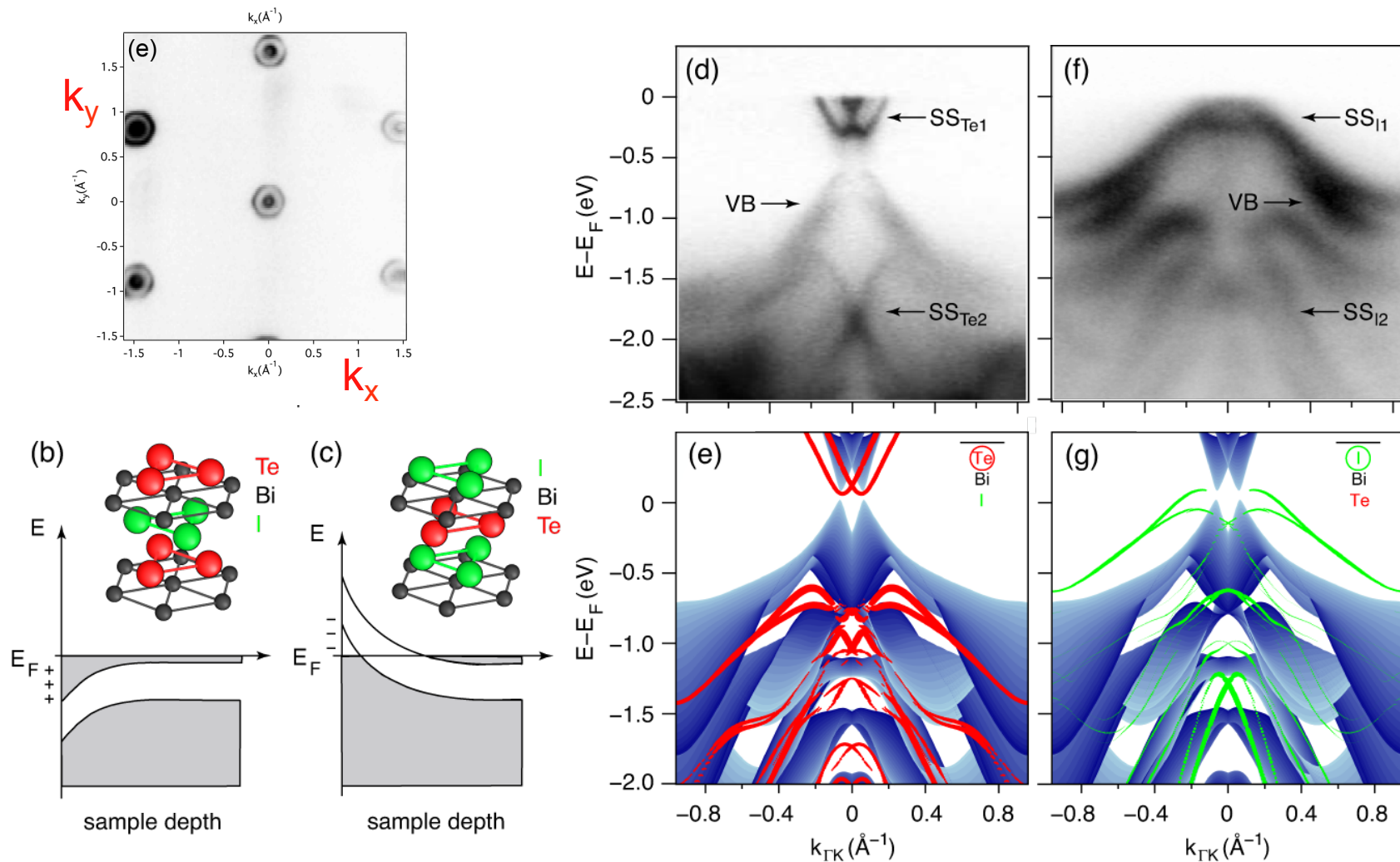
**Rashba spin pattern**

K. Ishizaka et al., Nature Mat. **10**, 521 (2011)

# More intriguing: two surface terminations



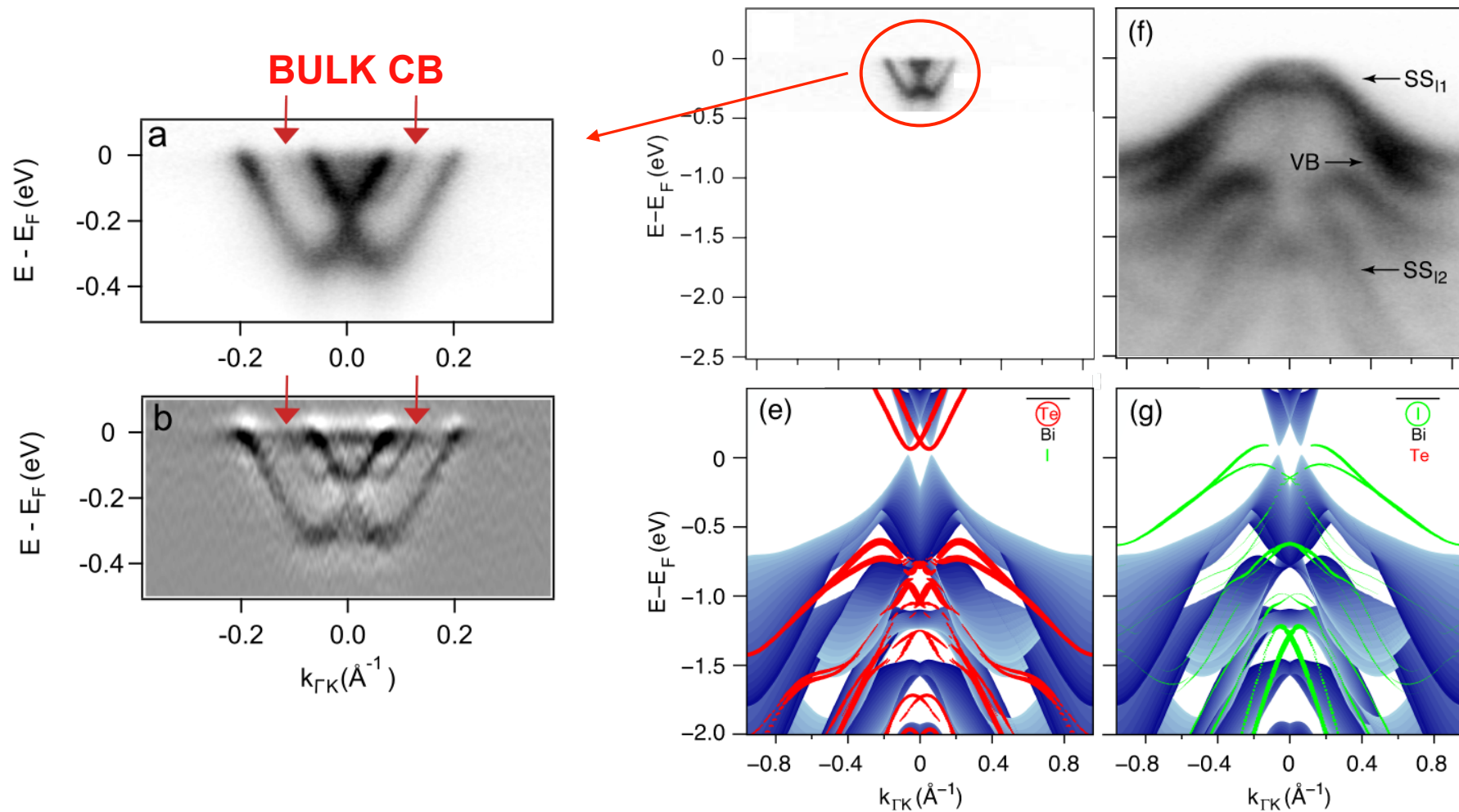
# Ambipolar Rashba effect



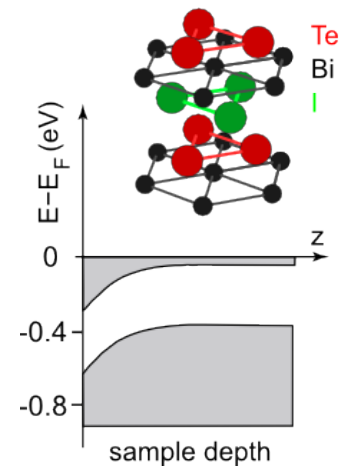
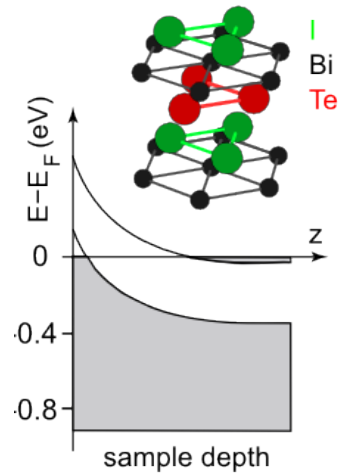
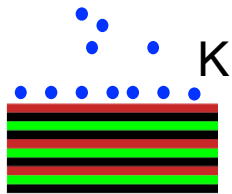
DFT + GGA (no band bending)

A. Crepaldi et al., PRL **109**, 096803 (2012)

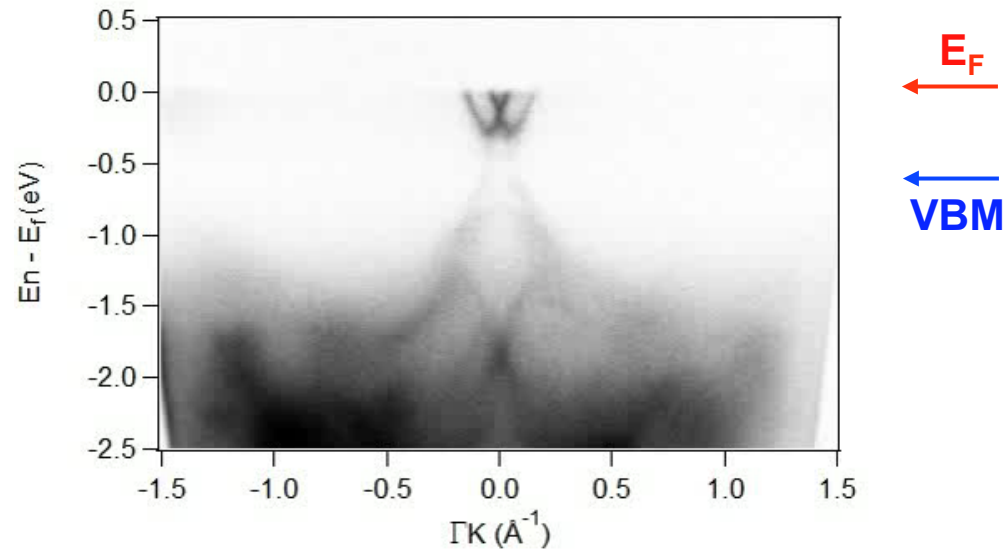
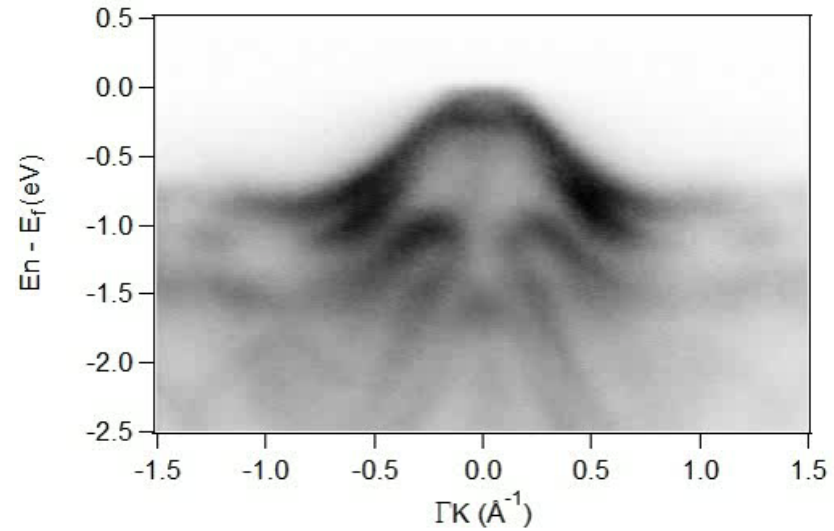
# Surface AND bulk states



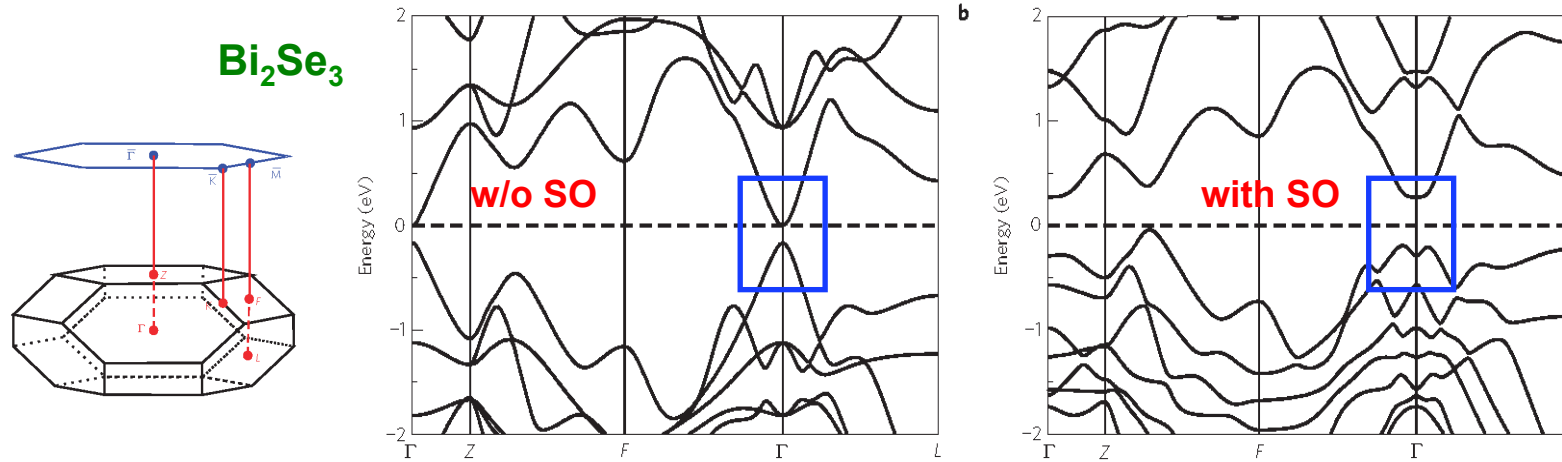
# Tuning the band bending by surface doping



K doping

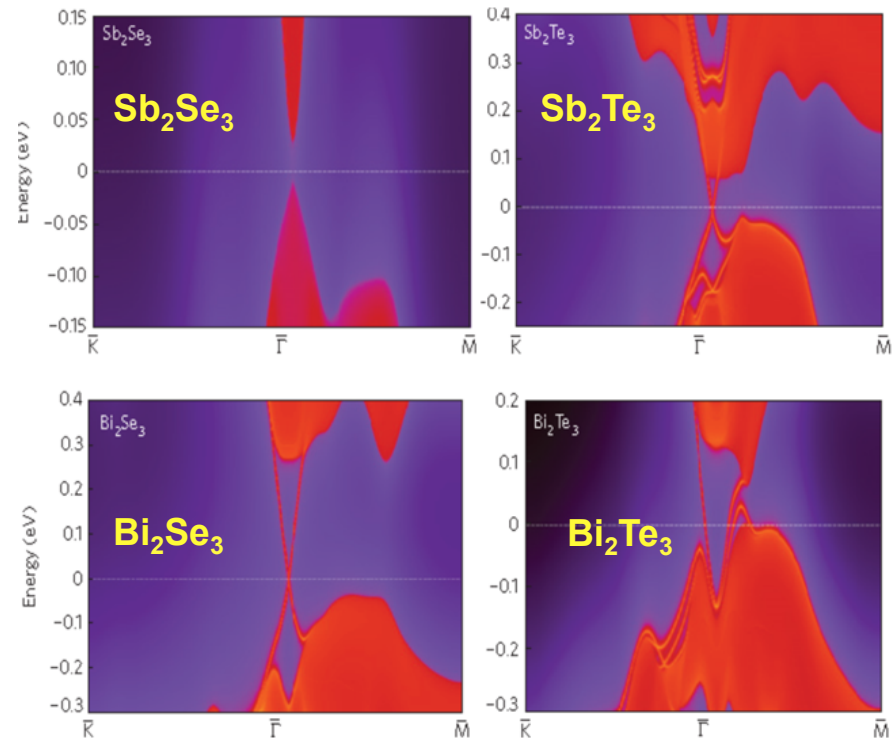


# The SO interaction switches bands around the gap



Sb <sub>2</sub> Se <sub>3</sub>	+ - + - + - + - + - + - - - ; +	(+)
Sb <sub>2</sub> Te <sub>3</sub>	+ - + - + - + - + - + - - - ; +	(-)
Bi <sub>2</sub> Se <sub>3</sub>	+ - + - + - + - + - + - - - ; +	(-)
Bi <sub>2</sub> Te <sub>3</sub>	+ - + - + - + - + - + - - - ; +	(-)

parity switching



H. Zhang et al., Nature Phys. **5**, 438 (2009)

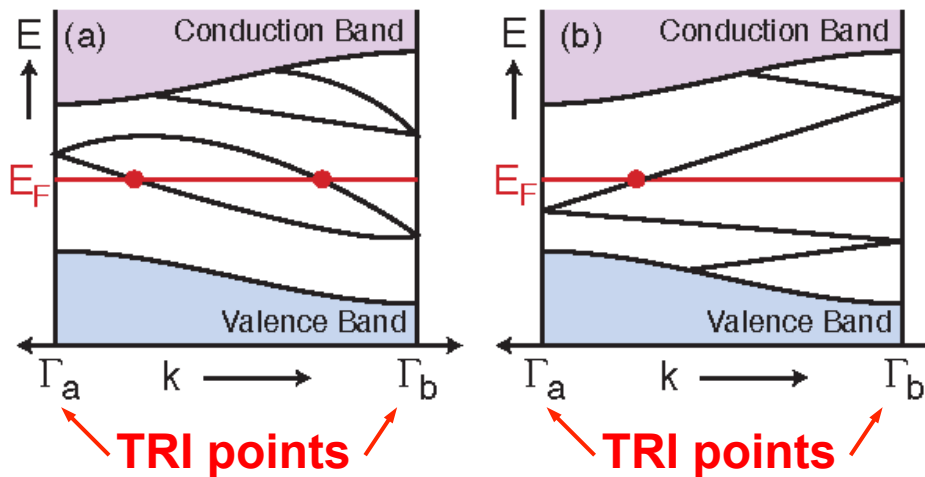
# “Edge states” in 3D insulators

“Trivial” and topological insulators differ in a topologically invariant quantity (related to the symmetry properties of the wavefunctions)

Surface states: partner switching

Trivial

Non-trivial

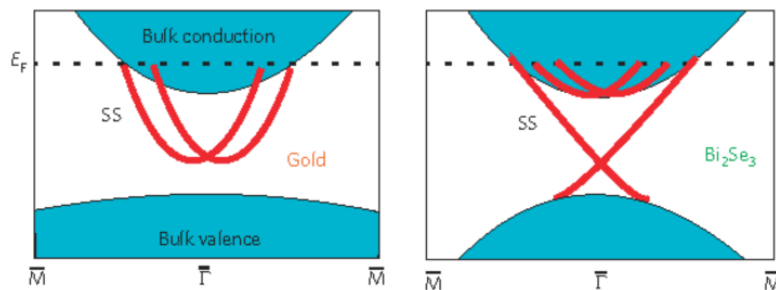


TRI points

TRI points

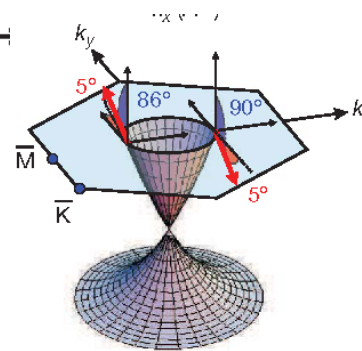
“Something” must happen at the Interface between a non-trivial and a trivial (e.g. the vacuum) insulator

Metallic states appear at the surface

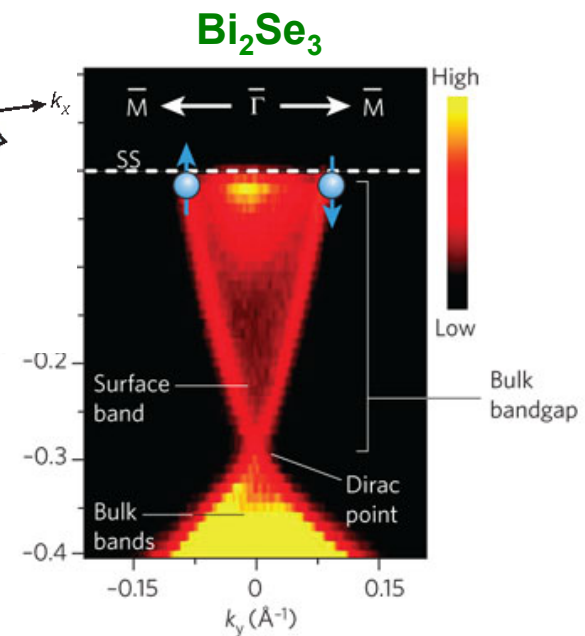


Au(111) - trivial

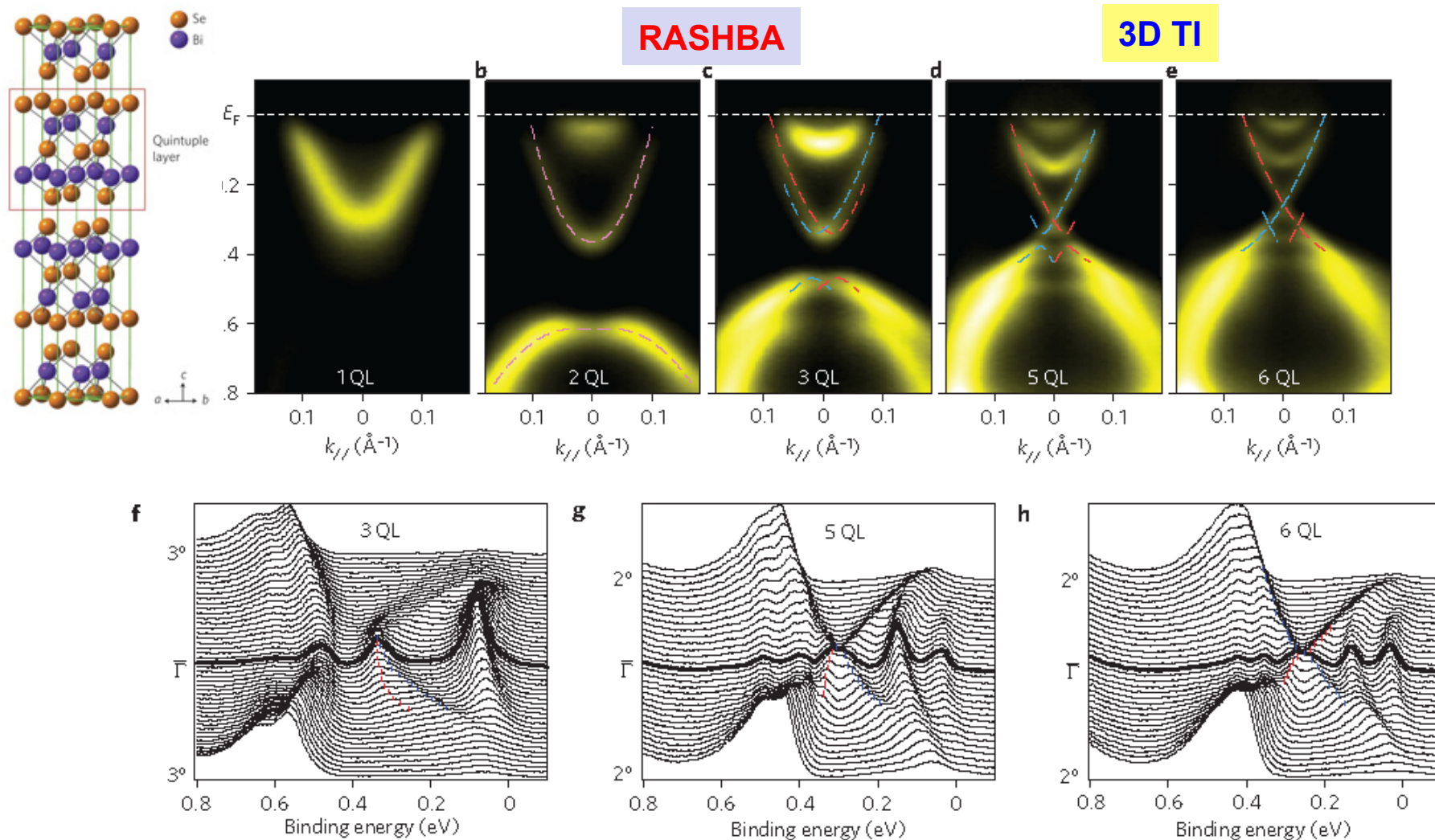
$\text{Bi}_2\text{Se}_3$



A single Dirac cone



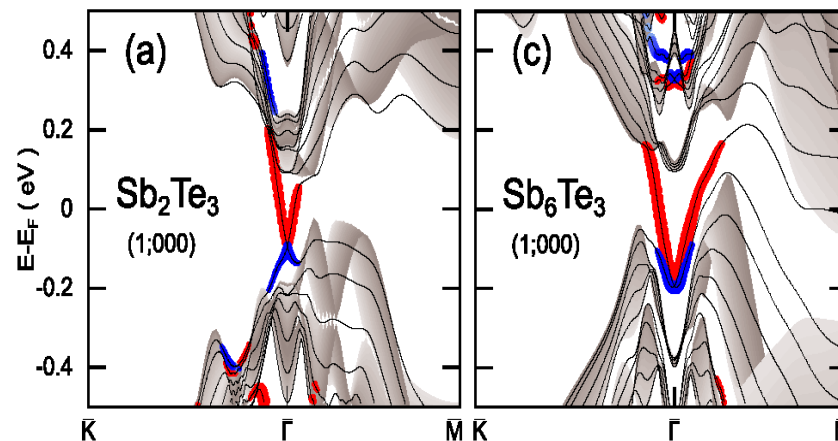
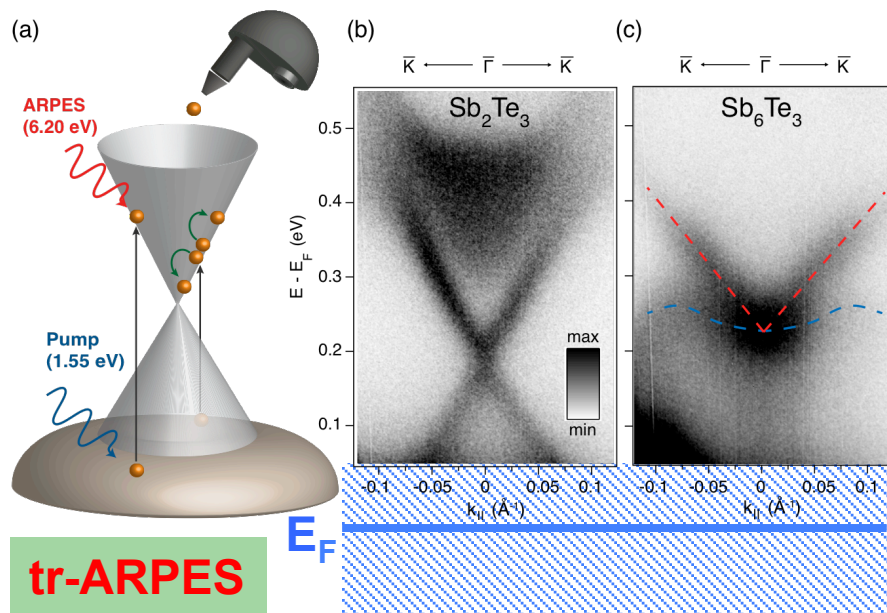
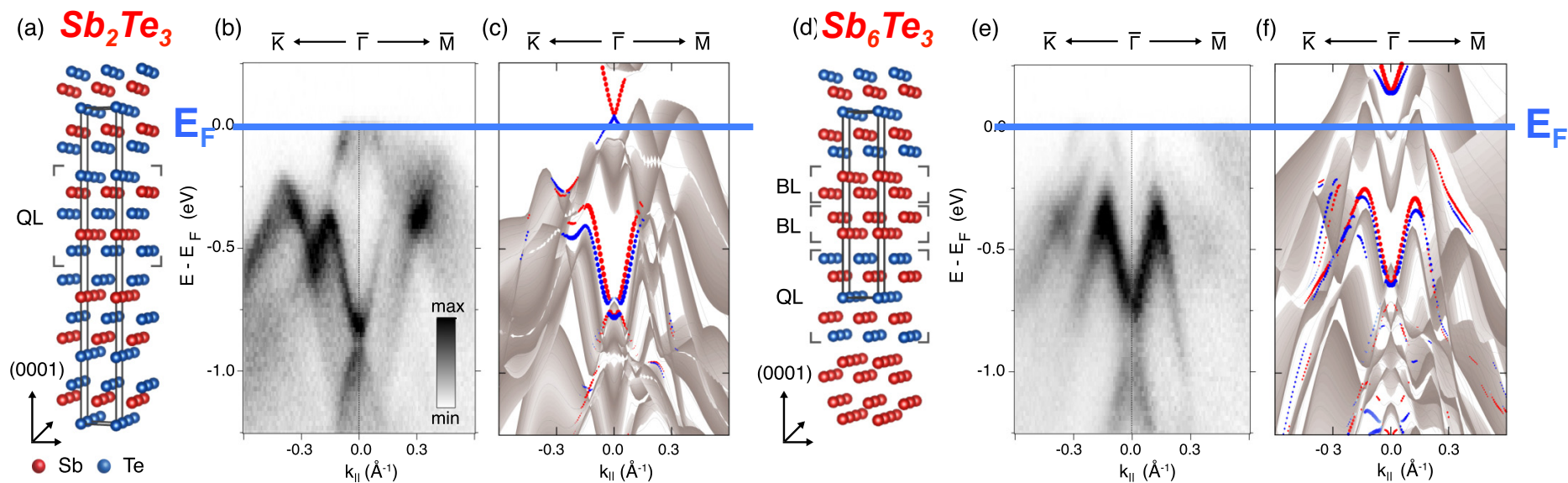
# Bi<sub>2</sub>Se<sub>3</sub> thin films: from Rashba to TI layer-by-layer



Yi Zhang et al., Nature Phys. **6**, 584 (2010)

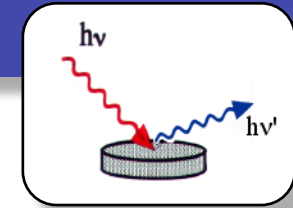


# Pumping electrons into the empty states: tr-ARPES

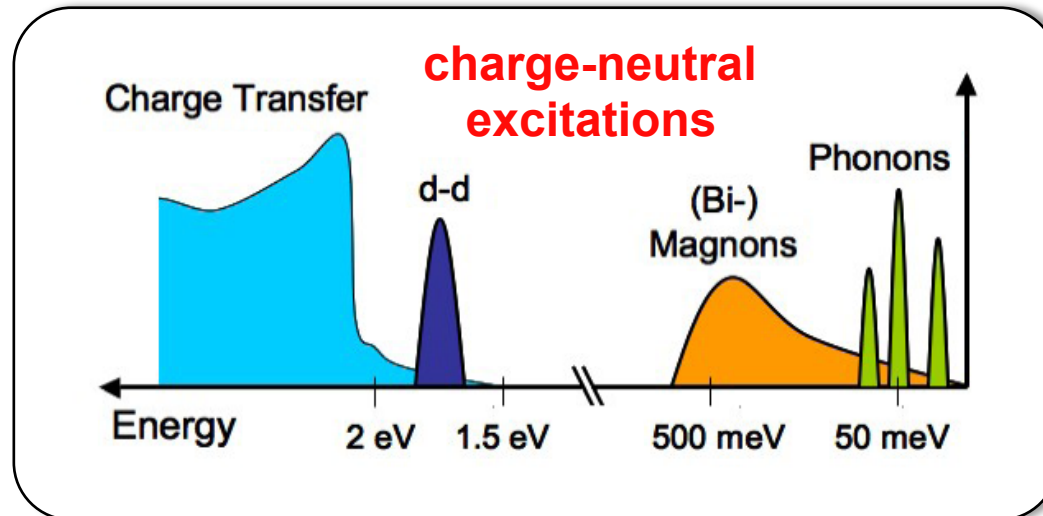


Johansen et al., PRB 91, 211001 (2015)

# RIXS: optics...with a twist



## RIXS probes multiple energy scales



Chemical selectivity from core hole, but the final state has no core hole → **high resolution**

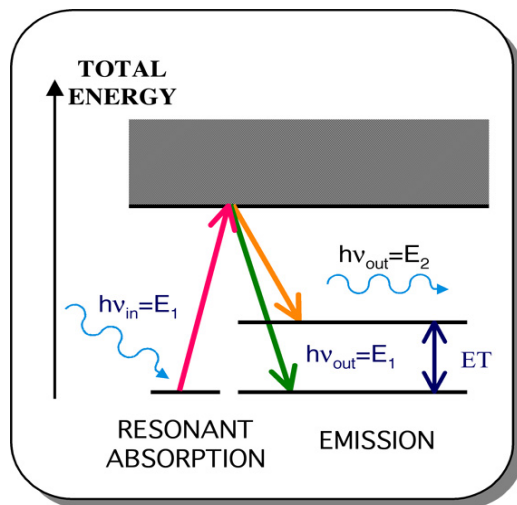
**q dependence**

Photon in - photon out: OK for insulators; external fields

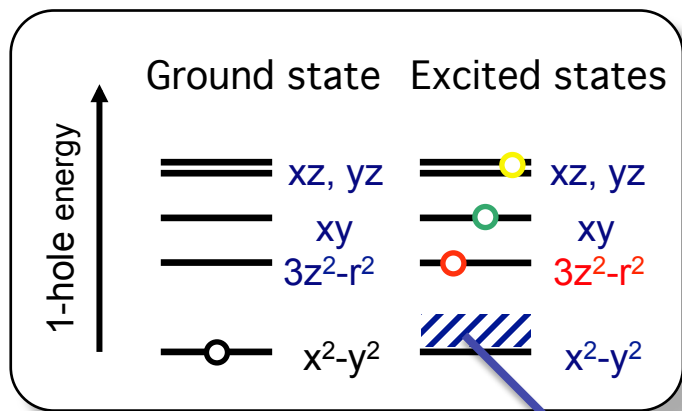
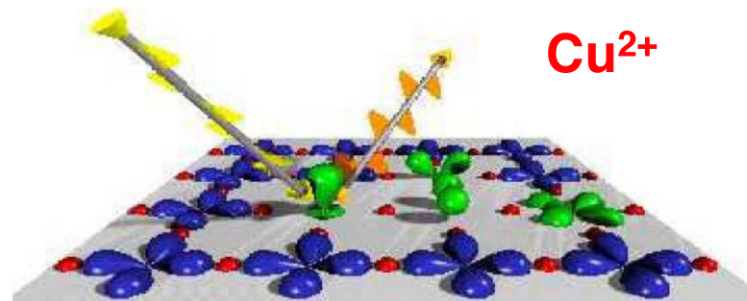
***Sensitive to spin excitations***

# RIXS: Raman with x-rays

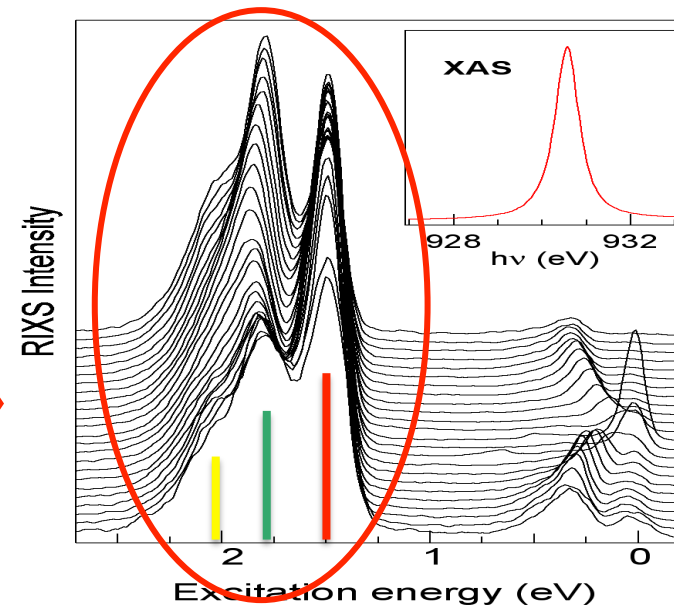
**$L_{2,3}$  edges  $2p \rightarrow 3d$  ; directly probes the  $d$  states**



**$\text{Cu}^{2+}$**



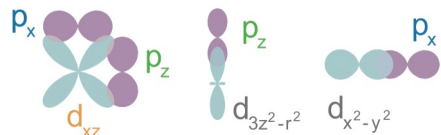
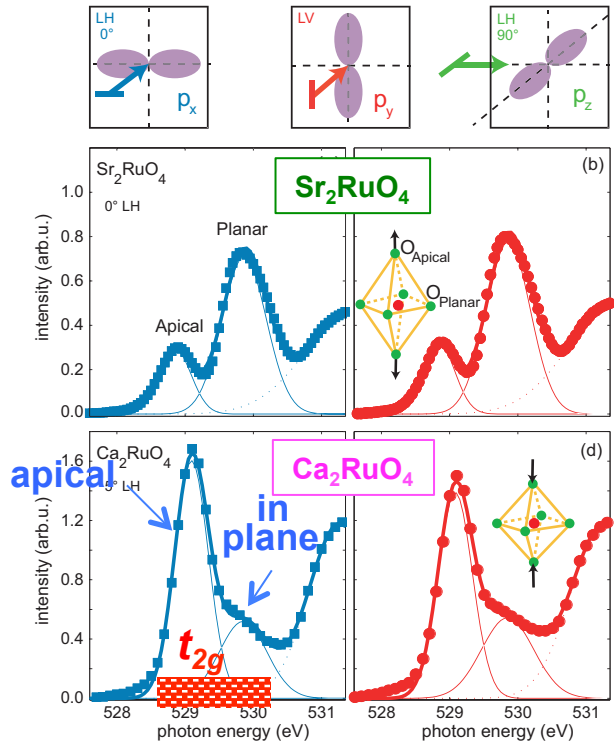
Collective excitations



# Ruthenates...again – RIXS probes inter- $t_{2g}$ excitations

Fatuzzo et al., PRB (2015)

**O 1s XAS**



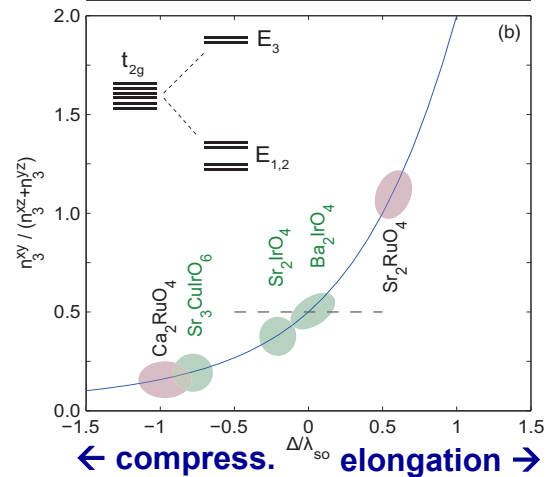
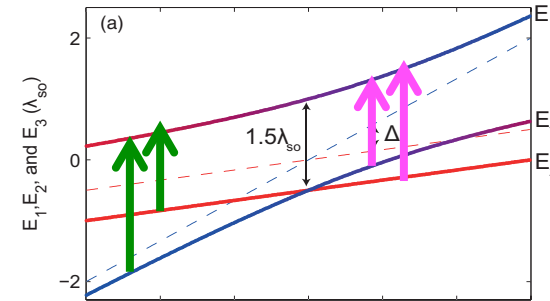
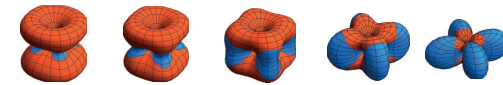
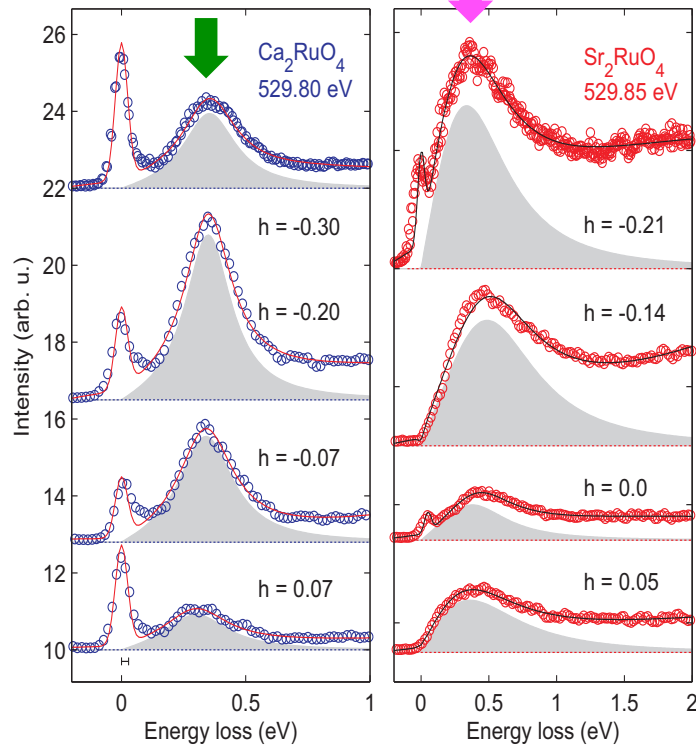
**in-plane:**

$p_x \rightarrow xy$ ;  $p_y \rightarrow xy$ ;  $p_z \rightarrow xz, yz$

**Apical:**

$p_x \rightarrow xz$ ;  $p_y \rightarrow yz$

**$t_{2g}$  excitations** **O 1s RIXS**

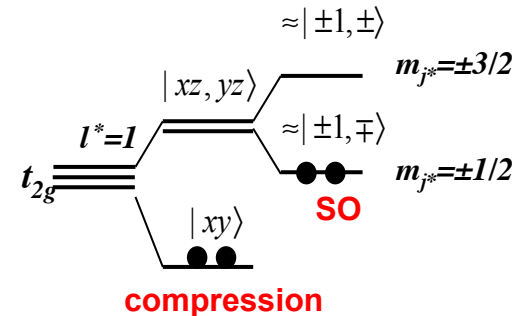


XAS  $\rightarrow n^{xy}/(n^{xz}+n^{yz})$

Model  $\rightarrow \Delta/\lambda_{SO}$

RIXS  $\rightarrow \Delta; \lambda_{SO}$

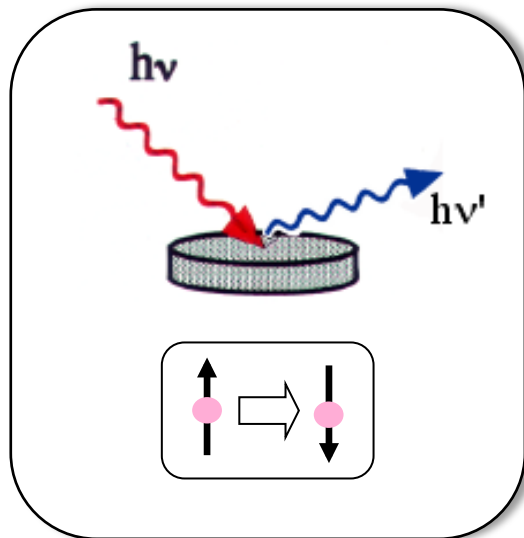
**$\lambda_{SO}=200$  meV (both)**



**compression**

# Low-energy excitations: spin flips

Photons do not couple directly to spins, but...



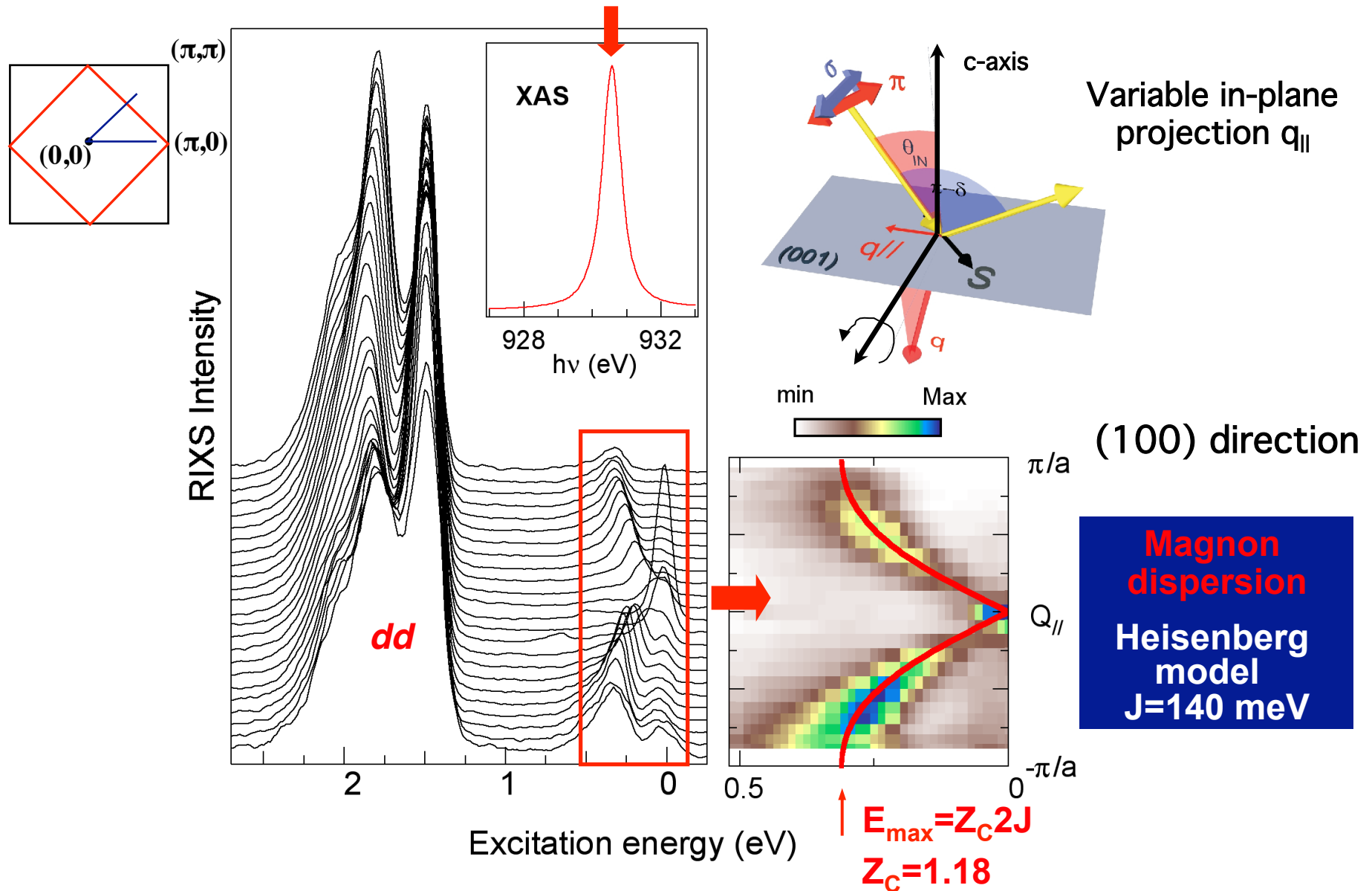
$$\Delta E_{so}(2p) \sim 20 \text{ eV}$$

- F.M.F. De Groot et al., PRB 57, 14 548 (1998)
- LJP Ament et al., PRL 103, 117003 (2009)
- MW Haverkort, PRL 105, 167404 (2010)
- T. Nagao and J. Igarashi, PRB 85, 224436 (2012)

Spin-orbit is large in the intermediate state.  
S is not a good quantum number  
 $\Delta S_z \neq 0$  transitions are possible !

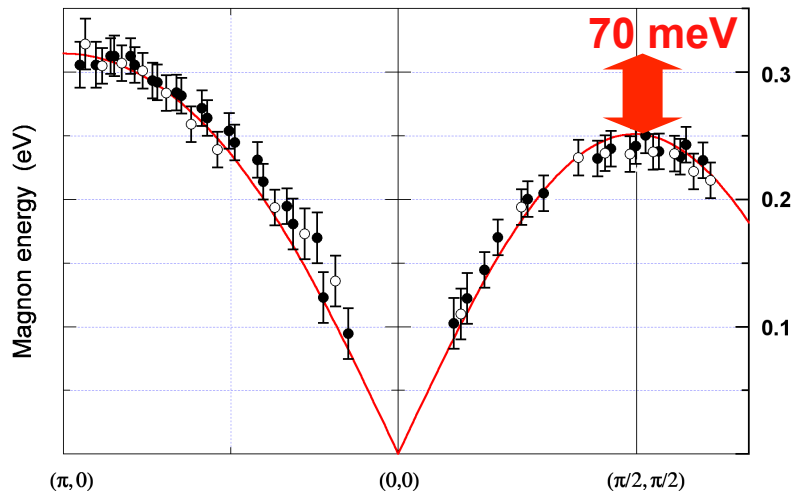
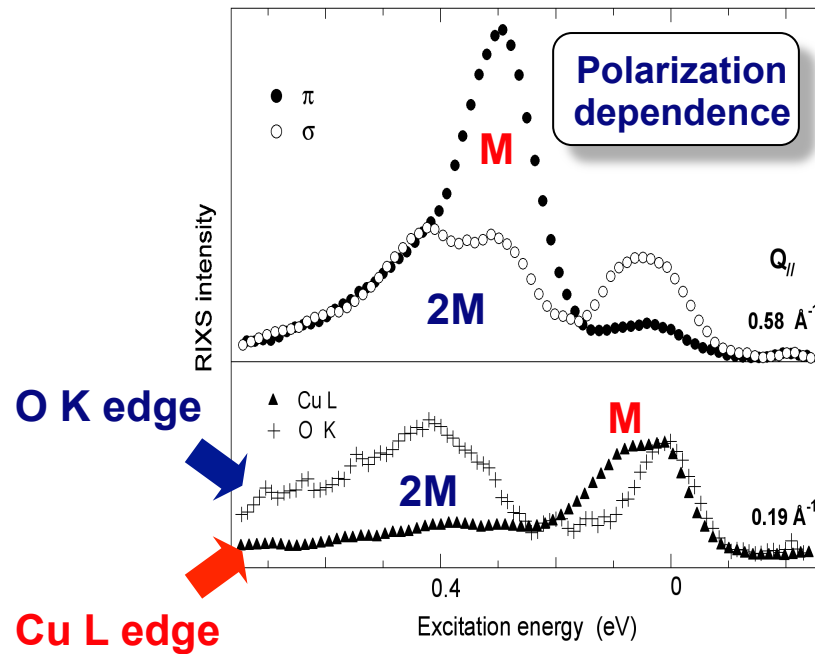
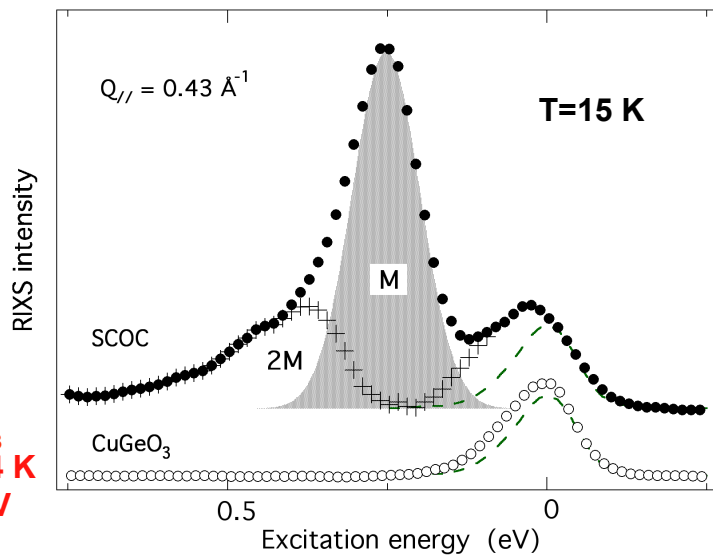
➔ One flipped spin NOT an eigenstate for the solid: dispersion

# Magnons in a 2D $S=1/2$ Heisenberg AF: $\text{Sr}_2\text{CuO}_2\text{O}_2$

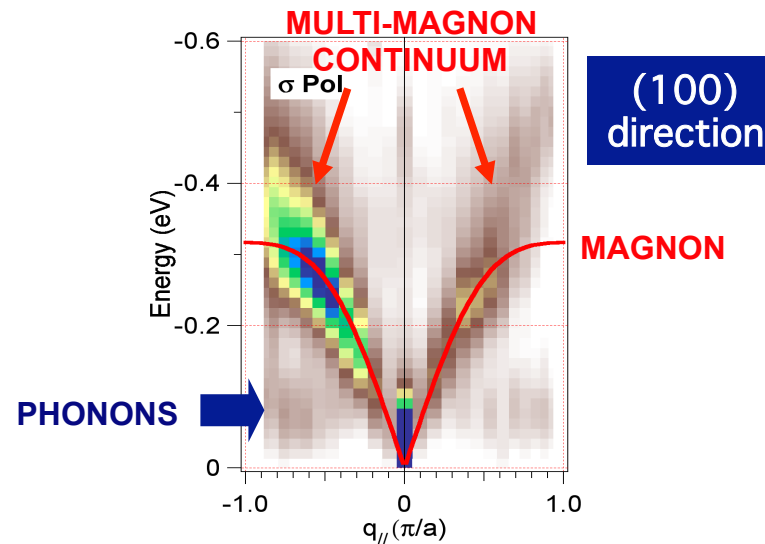


# Line shape analysis of the magnetic excitations

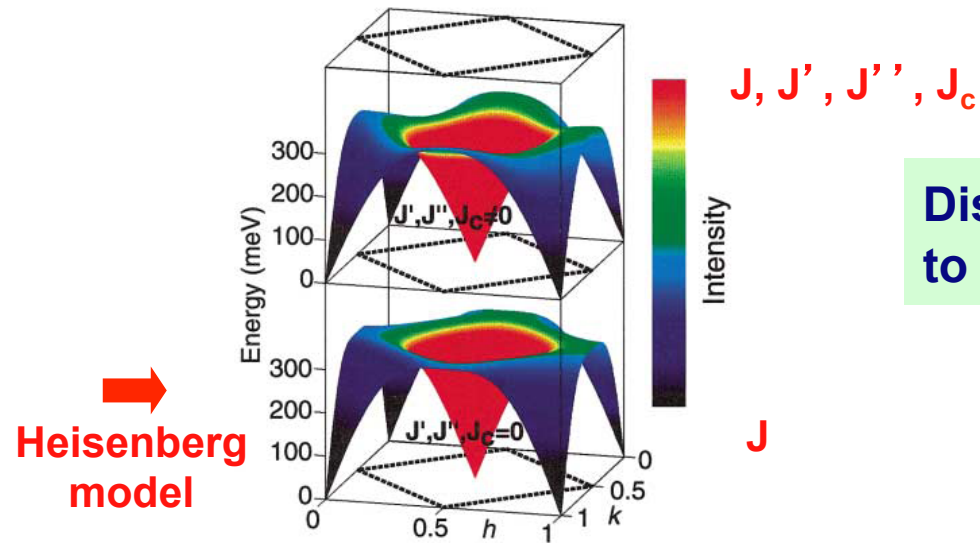
**CuGeO<sub>3</sub>**  
**T<sub>SDW</sub>=14 K**  
**J=5 meV**



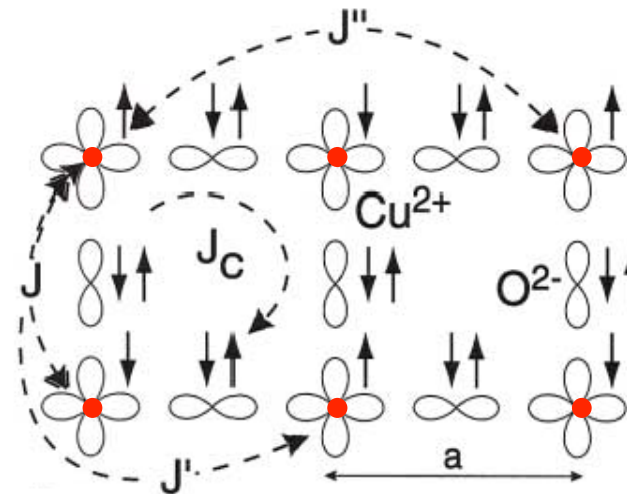
**Large dispersion along AFM BZ boundary**



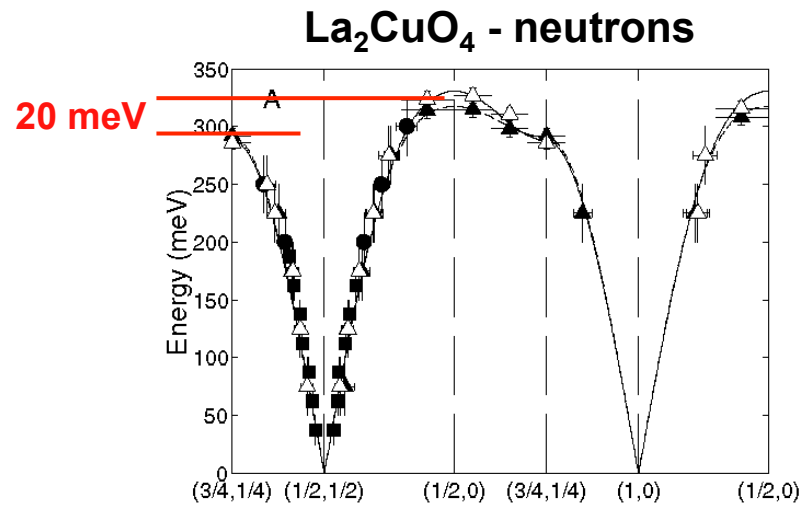
# MBZ boundary dispersion: why is it interesting ?



Dispersion along MBZ boundary is due to exchange interactions beyond NN



Notice: sub-mm samples !



R. Coldea et al., PRL 86, 5377 (2001); N.S. Headings et al., PRL 105, 247001 (2010)

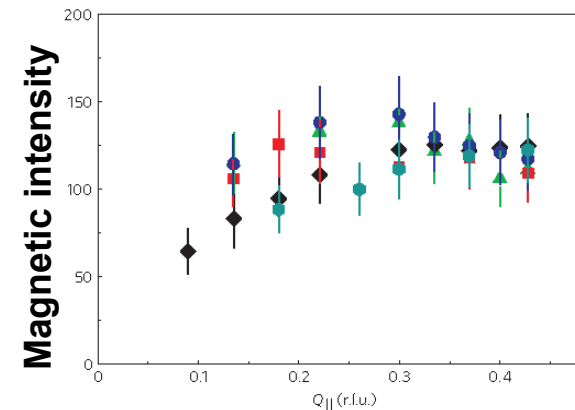
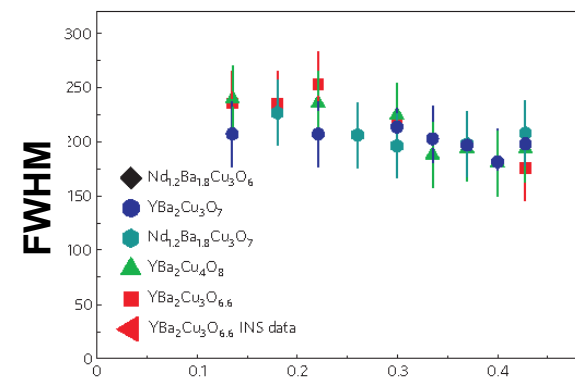
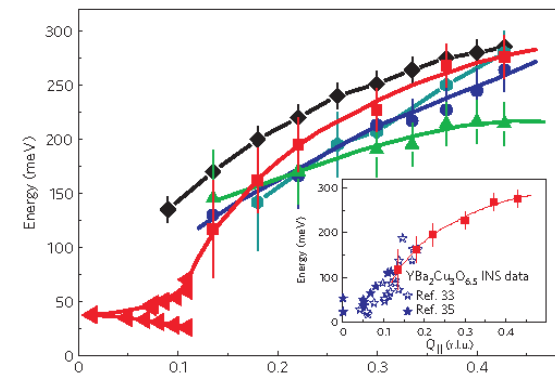
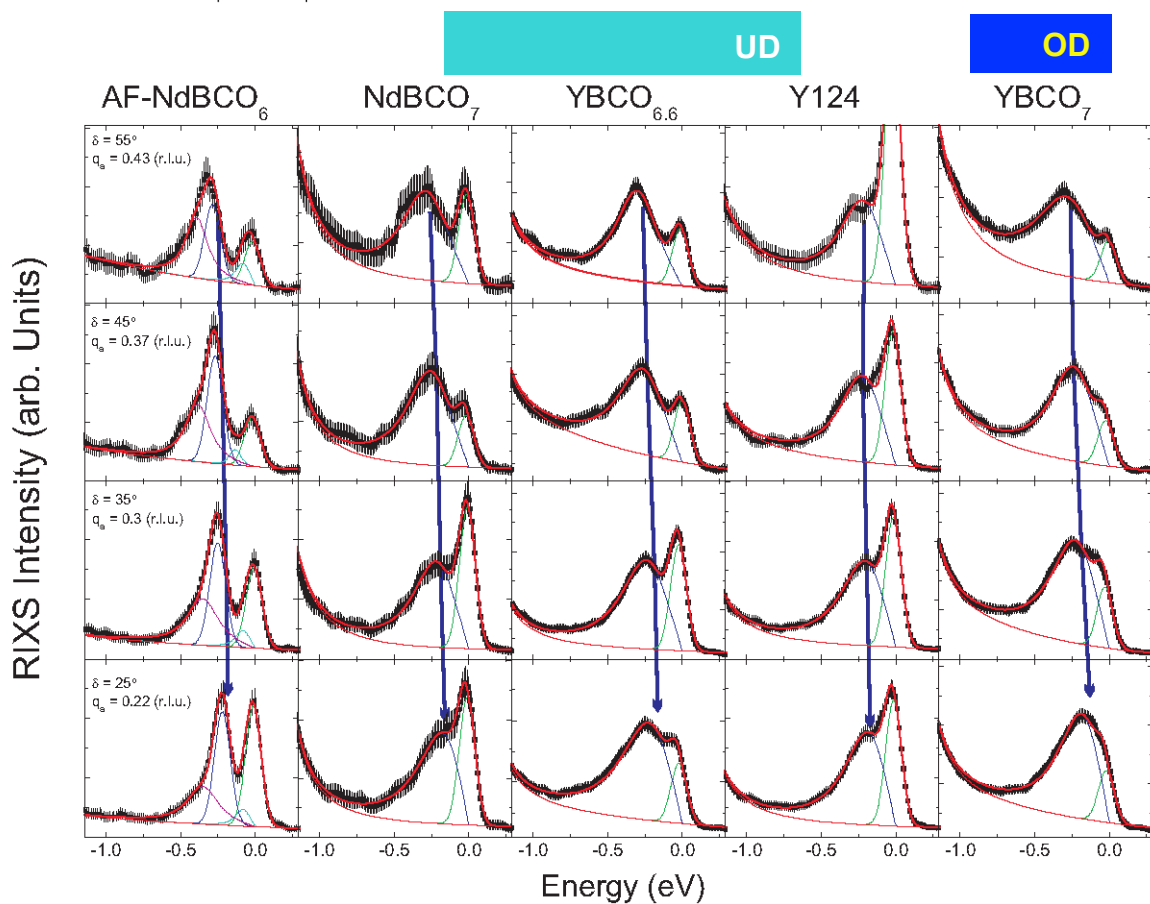


# Paramagnons in the doped cuprates

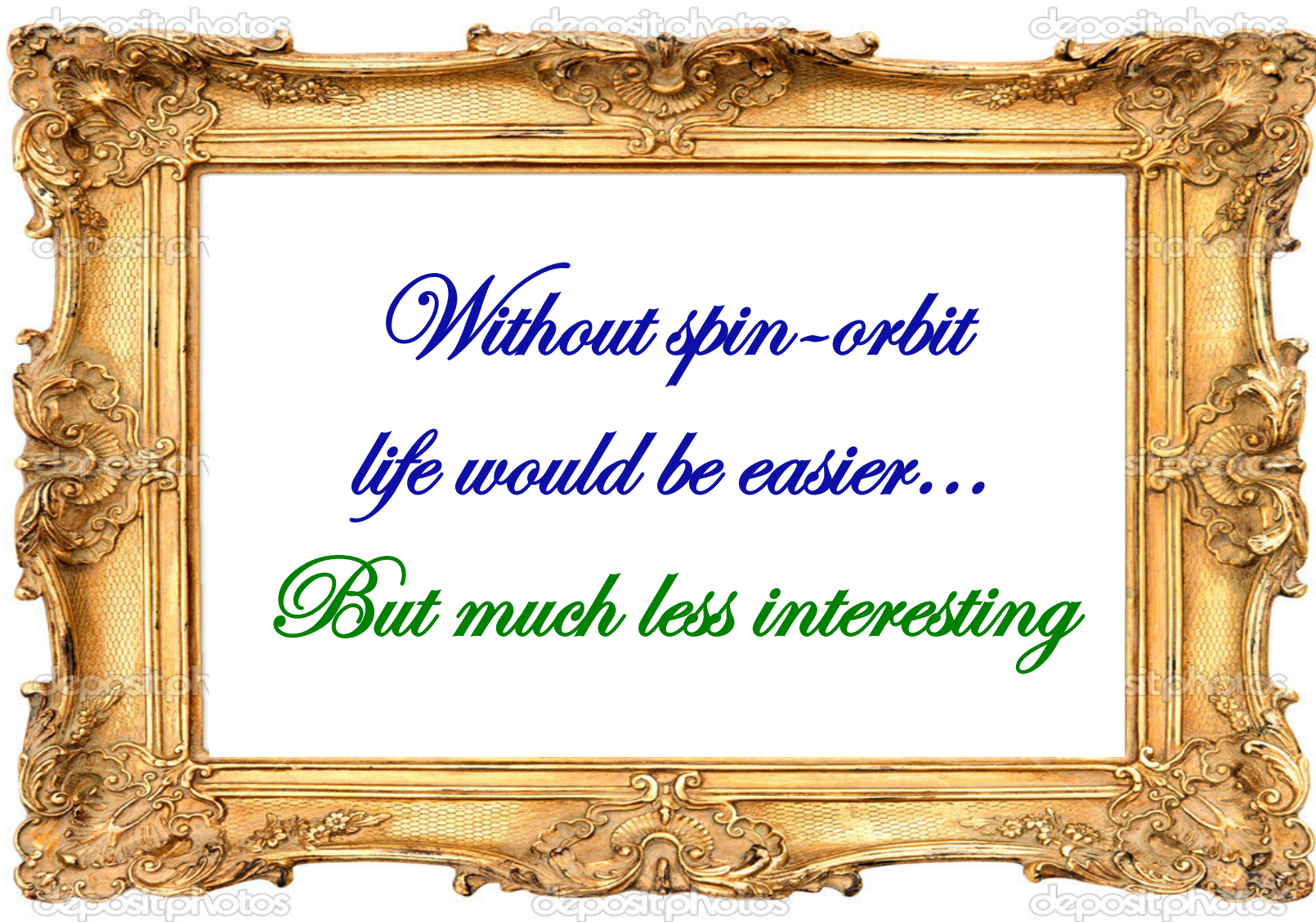
## Intense paramagnon excitations in a large family of high-temperature superconductors

M. Le Tacon<sup>1\*</sup>, G. Ghiringhelli<sup>2</sup>, J. Chaloupka<sup>1</sup>, M. Moretti Sala<sup>2</sup>, V. Hinkov<sup>1,3</sup>, M. W. Haverkort<sup>1</sup>, M. Minola<sup>2</sup>, M. Bakr<sup>1</sup>, K. J. Zhou<sup>4</sup>, S. Blanco-Canosa<sup>1</sup>, C. Monney<sup>4</sup>, Y. T. Song<sup>1</sup>, G. L. Sun<sup>1</sup>, C. T. Lin<sup>1</sup>, G. M. De Luca<sup>5</sup>, M. Salluzzo<sup>5</sup>, G. Khaliullin<sup>1</sup>, T. Schmitt<sup>4</sup>, L. Braicovich<sup>2</sup> and B. Keimer<sup>1\*</sup>

NATURE PHYSICS | VOL 7 | SEPTEMBER 2011



# Conclusion



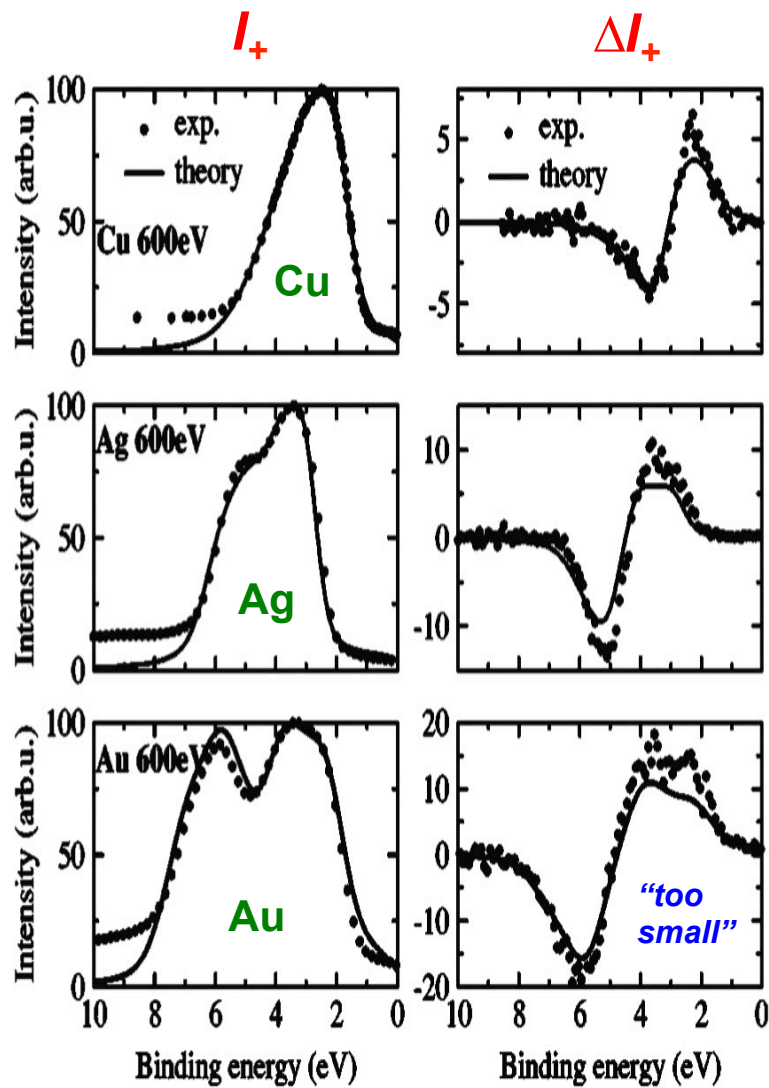
*Without spin-orbit  
life would be easier...*

*But much less interesting*

# References

- F.M.F. de Groot et al., Phys. Rev. B **40**, 5715 (1989).
- U. Fano, Phys. Rev. **178**, 131 (1969).
- C. Fatuzzo et al., Phys. Rev. B **91**, 155104 (2015).
- J. Kessler, *Polarized Electrons 2<sup>nd</sup> ed.*, Springer Series on Atoms and Plasmas, Vol. 1 (1985)
- J. Kirschner, Polarized Electrons at Surfaces, Springer Tracts in Modern Physics, Vol. 106 (1985)
- F. Clerc et al., J. Phys.: Condens. Matt. **16**, 3271 (2004)
- J. Stöhr and H.C. Siegmann, "Magnetism", Springer Solid-State Sciences (2006)
- T. Mizokawa et al., Phys. Rev. Lett. **87**, 077202 (2001)
- B.T. Thole and G. van der Laan, Phys. Rev. Lett. **67**, 3306; Phys. Rev. B **44**, 12424 (1991)
- G. van der Laan and B.T. Thole, Phys. Rev. B **48**, 210 (1993)
- C. De Nadai et al., Phys. Rev. B **70**, 134409(2004)
- C.N. Veenstra et al., Phys. Rev. Lett. **112**, 127002 (2014)
- S. Moser et al., N. J. Phys. **16**, 013008 (2014)
- Y. A. Bychkov and E. I. Rashba, JETP Lett. **39**, 78 (1984)
- M. Hoesch et al., Phys. Rev. B **69**, 241401(R) (2004)
- C.R. Ast et al., Phys. Rev. Lett. **98**, 186807 (2007)
- L.J.P. Ament et al., Rev. Mod. Phys. **83**, 705 (2011)
- F.M.F. De Groot et al., Phys. Rev. B **57**, 14 548 (1998)
- M. Guarise et al., Phys. Rev. Lett. **105**, 157006 (2010)
- M. Le Tacon et al., Nat. Phys. **7**, 725 (2011)

# Spin-orbit spectrum: *caveats*



C. De Nadai (2004)

